

Title: Growth and Inequality: Model Evaluation Based on an Estimation-Calibration Strategy

Authors: Hyeok Jeong and Robert Townsend

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1 **GROWTH AND INEQUALITY:**
2 **MODEL EVALUATION BASED ON**
3 **AN ESTIMATION-CALIBRATION**
4 **STRATEGY**

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9 **HYEOK JEONG**
10 *University of Southern California*

11 **ROBERT M. TOWNSEND**
12 *University of Chicago*

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16 This paper evaluates two well-known models of growth with inequality that have explicit
17 micro underpinnings related to household choice. With incomplete markets or
18 transactions costs, wealth can constrain investment in business and the choice of
19 occupation and also constrain the timing of entry into the formal financial sector. Using
20 the Thai Socio-Economic Survey (SES), we estimate the distribution of wealth and the
21 key parameters that best fit cross-sectional data on household choices and wealth. We then
22 simulate the model economies for two decades at the estimated initial wealth distribution
23 and analyze whether the model economies at those micro-fit parameter estimates can
24 explain the observed macro and sectoral aspects of income growth and inequality change.
25 Both models capture important features of Thai reality. Anomalies and comparisons
26 across the two distinct models yield specific suggestions for improved research on the
27 micro foundations of growth and inequality.

28 **Keywords:** Growth and Inequality, Wealth-Constraints, Self-Selection, Occupational
29 Choice, Financial Deepening

30
31 **1. INTRODUCTION**

32
33 Our purpose is to understand growth and inequality. We do this through an evaluation
34 of macro models that are explicit about micro underpinnings and impediments
35 to trade. We use the explicit structure of the macro models to make exact numerical
36 predictions for aggregate dynamics, the dynamics of key subgroups, and end-of-
37 sample period income distributions. We compare these predictions to those objects
38 in the data from a given, selected country. In this sense, we take theory seriously as

39
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Jeong, Department of Economics, University of Southern California, 3620 S. Vermont Ave., Kaprielian Hall Room
300, Los Angeles, CA 90089, USA; e-mail: hjeong@usc.edu.

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1 in the calibration, real business cycle literature, pioneered by Kydland and Prescott
2 (1982). However, the parameters of preferences, technology, and distribution of
3 shocks that we use are neither arbitrarily chosen nor borrowed from other studies.
4 Rather, we explicitly estimate the key parameters using the models' micro under-
5 pinnings, which presuppose that household and business choices are constrained
6 by wealth. Specifically, we use repeated cross-sections of micro data from the
7 country that we study to estimate most of these key parameters, using maximum
8 likelihood methods on the household and business choices.

9 In the growth and inequality literature, tight links between theory and data
10 are rarely pursued. Various equilibrium theories of growth and inequality have
11 been developed without evaluating their empirical validity. Until recently, studies
12 of the empirical relationship between growth and inequality are mostly based on
13 cross-country regression analysis. The results of these reduced-form cross-country
14 studies are, unfortunately, robust neither to the specification of estimation nor to
15 the selection of data, and have provided only suggestive clues.¹ A more natural
16 alternative for studying the dynamic relationship between growth and inequality
17 is an analysis of the evolution of the income distribution for a given country over
18 time, using a series of micro data. Bourguignon (2002) makes an excellent case.

19 Our goal is both methodological and positive. The methodological goal is to
20 accomplish what we feel is a natural synthesis between theory and econometrics.
21 On the positive side, we use the method to discover where the models fit well and
22 where salient anomalies appear, to guide the construction of new and better models.
23 More generally, we hope that our model evaluation exercise might advance the
24 "mutual penetration of quantitative economic theory and statistical observation,"
25 as Frisch (1933) envisioned. In particular, we hope that this mutual penetration
26 helps to narrow the gap between "theory without measurement" and "measurement
27 without theory" in the growth-inequality literature.

28 Two immediate comments are in order. First, our merging of micro with macro in
29 both theory and estimation is sufficiently challenging that we try to stick to familiar
30 ground on other dimensions. Namely, we use two models that are reasonably well
31 known and presumably well understood and analyze each of the models against
32 micro and macro data as they stand, rather than leaping to an integrated model
33 that combines in one spot the salient features of the two models. The paper does
34 conclude with specific instructions for future model construction, incorporating
35 lessons learned from the model evaluation.

36 Second, we use neither the macro aggregate dynamics of growth and inequality
37 nor the shape of the income distribution in our estimation. These data are saved in
38 order to compare the models' macro dynamics predictions with those in the data.
39 We use model's implications of individual agents's choices only to fit the micro
40 data. This two-step procedure, setting aside some of the data for "verification" or
41 "testing," and excluding its use in "parameter selection," is a commonly established
42 practice in empirical work in the natural sciences. See Oreskes, Shrader-Frechette,
43 and Belitz (1994) and Hansen and Heckman (1996), for example, who provide a
44 lively discussion about this two-step procedure as an empirical strategy.

1 Our empirical strategy is based on the following reasoning. First, the separation
2 between verification and parameter selection helps us to avoid “overfitting” of
3 the model to the data, as Granger (1999) discusses. Second, we fit to the micro
4 data of household choices, not to the aggregate dynamics of growth and income
5 distributions, because we consider household choices as the (micro) foundation
6 of the objects that we want to explain, that is, macro dynamics of growth and
7 inequality.²

8 Here we apply our method to Thailand, a country that grew rapidly for the
9 1976–1996 period, but with increasing and then decreasing inequality. Real GNP
10 per capita grew at 5.7% annually. In particular, for the 1986–1996 period, the
11 average annual growth rate at 9% even exceeded those of neighboring East Asian
12 miracle economies. However, the already high-income Gini coefficient of Thailand
13 at 0.436 in 1976, close to the average-income Gini coefficient of sub-Saharan
14 African countries at 0.441, increased to 0.515 by 1996, exceeding the average
15 income Gini coefficient in Latin American and Caribbean countries at 0.502.³

16 Furthermore, we know from Jeong (in press) and from his use of the Thai
17 Socio-Economic Survey (SES) data that substantial parts of this growth with
18 changing inequality are accounted for by population shifts across subgroups and
19 associated changes in income gaps. As population shifts across sectors were
20 postulated by Kuznets (1955) to be the driving force of the relationship between
21 growth and income inequality, the focus on self-selection as a micro foundation
22 of growth and inequality is natural. Two key characteristics that account for the
23 changes are occupational shift and financial deepening. Thus, we adopt from
24 the literature two reasonably well-known models of growth and inequality that
25 emphasize one or the other of these self-selection components, although there
26 are other possible channels for growth and inequality.⁴ In the occupational choice
27 model of Lloyd-Ellis and Bernhardt (2000) (hereafter LEB), households of varying
28 talent face imperfect credit markets in financing occupational choice and the scale
29 of enterprise. Thus households are constrained by limited wealth, although this
30 can be alleviated over time. As the distribution of wealth evolves, so do the
31 occupational composition of population and income differentials, generating the
32 dynamics of growth with changing inequality. Likewise, in the financial deepening
33 model of Greenwood and Jovanovic (1990) (hereafter GJ), households face wealth
34 constraints in their decisions to undertake costly entry into the financial system
35 itself. Participation in financial intermediaries provides the benefits of sharing
36 idiosyncratic risks and advanced information on aggregate risks. As economy-wide
37 wealth shifts to the right, more households gain access to financial intermediaries,
38 and this in turn affects growth and inequality dynamics.

39 Until recently, neither model has been brought to actual data. Exceptions are
40 Gine and Townsend (2004) who estimated the LEB model and Townsend and Ueda
41 (2006) who calibrated the GJ model. Both papers study the aggregate implications
42 of the models. Here we study the decomposed subgroup dynamics and the shapes
43 of the implied income distributions as well as the aggregate dynamics of growth
44 and inequality. We also implement structural estimation using the explicit dynamic

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1 programs of the participants and nonparticipant subgroups of the GJ model. This is
2 different from the calibration exercise of Townsend and Ueda (2006). Furthermore,
3 our comparative evaluation of the two models with the same data addresses in
4 another way their empirical validity, and yields the instructions for future model
5 construction.

6 Section 2 provides an overview of Thai growth and inequality, and summarizes
7 the results of the model evaluation exercise. Section 3 describes the occupational
8 choice model including estimation, simulation, and its fit to macro dynamics, sub-
9 group dynamics, and end-of-sample-period income distribution. Section 4 follows
10 the same ordering for the financial choice model. Section 5 concludes.

11 2. OVERVIEW

12 2.1. Thai Background

13 Thai per capita income grew at 4.5% each year on average for the two decades
14 between 1976 and 1996, with low or slightly negative growth from 1976 to 1986,
15 surging to 12% in late 1980s, and then declining to 6% by 1996. The LEB model
16 economy captures the recession, surge, and decline, although the magnitudes are
17 smaller, for example, from 1% to 7% in the surge, and a decline to 2% after. Thai
18 income inequality (measured by Theil-L index) also grew at 2.4% each year and
19 displays a Kuznets curve, first increasing from 0.39 in 1976 to 0.66 in 1992, and
20 then declining to 0.58 by 1996. The model mirrors this movement in inequality
21 quite well, although it underpredicts the level throughout, specifically increasing
22 from 0.24 in 1976 to 0.50 in 1992, with a more dramatic and earlier decline to
23 0.33 by 1996. The Thai fraction of the population who are either self employed
24 or hire workers was virtually constant around 15% for the period of 1976–1990
25 and then increased to 19% during 1991–1996. The model economy captures these
26 dynamics as well, although again the levels are lower.

27 The fraction of wage earners who are not in the financial sector declined steadily
28 in the Thai economy from 80% to 60%, and the LEB model economy imitates
29 this decline, from 90% to 70%. The fractions of financial sector wage earners and
30 entrepreneurs rise from 5% to 21% and 2% to 6%, respectively, almost exactly as
31 in the model. There are in the data many entrepreneurs among those participating
32 in the financial sector, about 21% on average, although in the model this is higher,
33 28% on average. But in the data, 15% of those in “autarky” (i.e., nonfinancial
34 sector) are also entrepreneurs, whereas it is only 2% in the model.

35 Wage earners who do not participate in the financial sector earn the least and their
36 earnings are more or less constant until late 1980s, but their earnings increase in
37 the 1990s. The model imitates this pattern. The highest-earning group in Thailand
38 are financial sector participants, especially those running enterprises, whereas
39 the highest-earning group in the model economy are entrepreneurs, especially
40 nonparticipants. There is also much co-movement in earning growth across all
41 sectors in Thailand, whereas in the model, movements of the wage and interest
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1 rate cause divergence. In Thailand, the entrepreneurial premium, the ratio of profits
2 relative to wages, is high at almost 2 in 1976, and this declines to 1.6 by 1996. In
3 the model, the premium is overdone and the decline even more dramatic, from 20
4 to 8.

5 Inequality in Thailand, by 1986 and beyond, is highest among participant en-
6 trepreneurs, ranging overall from 0.45 to 0.70. In the model, that group also has the
7 highest level of inequality, but the level is lower at 0.15 on average. The dynamics
8 of aggregate inequality is captured well by the model via changes in across-group
9 inequality.

10 In Thailand, the population shifts from wage earners to entrepreneurs, and from
11 nonparticipants in financial sector to participants, contribute 1.6% of the total
12 4.5% of annual per capita income growth. This leaves 64% of growth attributed to
13 within-subgroup growth. Occupational shifts alone, ignoring changes in financial
14 participation status, account for one-tenth of the compositional effect on growth.
15 The joint compositional effects on growth in the model is larger at 3.6%.

16 Of the total inequality growth rate at 2.4% per year in Thailand, 0.6% is a
17 result of population shifts into higher income categories, -0.02% because of
18 income convergence across subgroups, and 0.14% because of population shifts into
19 higher inequality categories. The rest, 1.7% , is from the inequality changes within
20 subgroups. Put differently, in Thailand 70% of inequality change is not accounted
21 for by these occupation/financial sector categories. In the model, the signs are
22 correct, but the orders of magnitude are not. Of the total predicted inequality growth
23 at 1.7% , 6.9% is because of population shifts into higher income categories, -3.8%
24 because of income convergence across subgroups, 0.3% because of population
25 shifts into higher inequality categories, and 0.1% because of the inequality changes
26 within subgroups. Essentially, the majority of the inequality change in Thailand
27 is within categories, whereas in the model, it is across categories.

28 The LEB occupational choice model predicts much higher concentration at the
29 lower left tail of the income distribution and hence more poverty than in the data.
30 Because of this difference, Kolmogorov-Smirnov test of goodness of fit for the
31 end-of-sample-period income distribution rejects the resemblance of the shape of
32 income distribution between the LEB model and the Thai data.

33 The Thai financial sector deepened in the sense that the population fraction
34 of the participants in the formal financial intermediaries increased from 6.4% to
35 26.6% for the two decades, in particular with nonlinear acceleration during the
36 1986–1996 period. The GJ financial deepening model gets the trends of financial
37 deepening, income growth, and inequality increase almost exactly. However, the
38 model misses some dynamics of the data, for example, the downturn in inequality
39 after 1992 and the 1986–1996 surge in financial deepening.

40 The income levels of Thai financial sector participants are higher than nonpar-
41 ticipants, at an initial ratio of 2.3, rising to 3.1 in 1992, then falling back to 2.4 by
42 1996. In the financial deepening model, the gap is continuously increasing, and
43 the premium is overdone, rising from 5 to 7. There is much more co-movement
44 of growth between the financial and nonfinancial sectors in the data than in the

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1 model, despite aggregate shocks in the model. Inequality is lower among partici-
2 pants only during 1979–1987 in Thailand, whereas in the model inequality among
3 participants is lower than the nonparticipants throughout, rising from 0.02 to 0.2.

4 In contrast to the small effects of occupational transition on growth, financial
5 deepening contributed to Thai income growth at 1.6% each year, 36% of total
6 annual growth. Its effects on Thai income inequality also were substantial, con-
7 tributing to 0.83% of inequality growth each year, 34% of the total inequality
8 growth (combining the effects resulting from population shifts into higher-income
9 categories and into higher-inequality categories). The GJ model predicts substan-
10 tial effects of financial deepening on growth and inequality change as in the data
11 but too large in order of magnitudes, 3.3% for income growth, 1.3% for inequality
12 increase. Again, the major source of the Thai inequality increase is a result of
13 the increases within financial and nonfinancial sectors, 1.52% of increase each
14 year (63% of the total inequality growth). This effect in the GJ model is tiny at
15 -0.1% .

16 The model misses some variety among the poor, misses the very rich, and is
17 bimodal in predicting the 1996 Thai income distribution, but overall the predicted
18 income distribution is not statistically different from the actual Thai income using
19 the same Kolmogorov-Smirnov test statistic.

22 2.2. Comparative Model Evaluation

23 The underlying mechanisms driving growth are different between the two models.
24 GJ is an Ak type of growth model with aggregate shocks, and LEB is a typical neo-
25 classical growth model subject to diminishing returns without aggregate shocks.
26 The key selection characteristics are also different, occupational choice in LEB
27 and financial participation in GJ. Nevertheless, at parameter values that best fit the
28 assumed micro selection decisions, both models predict the aggregate dynamics
29 of growth and inequality change reasonably well.

30 Of course, there are remaining differences between these models. GJ fits the
31 inequality level better than LEB. But movements over time of average income
32 and income inequality are better captured by LEB than GJ, without aggregate
33 shocks, through endogenous factor price movements. Evidently, the modeling of
34 endogenous movements of wages and interest rates is important. However, we
35 would not underplay the importance of aggregate shocks. In fact, there are strong
36 co-movements in growth rates across subgroups in the data (except the catchup
37 growth periods in the early 1990s). But both models fail to capture these co-
38 movements. Again, LEB simply lacks aggregate shocks. GJ does have aggregate
39 shocks in the risky technology, but the effects are asymmetric between nonpar-
40 ticipants and participants. The financial sector can mitigate the adverse effects of
41 aggregate shocks as they are foreseen. Nonparticipants are exposed to them, yet
42 they diversify into the low-yield safe technology. Thus in the end, co-movements
43 in growth rates across participant and non-participant groups are weak. Evidently,
44 we need another common factor that affects all subgroups, or we need to make

1 the informational advantage of the financial sector in forecasting aggregate shocks
2 less perfect.

3 Both models predict population shifts across key selection groups, from low-
4 income groups to high-income groups (entrepreneurs in LEB and financial sector
5 participants in GJ), and the effects of these compositional changes in the pop-
6 ulation on growth and inequality change are substantial, especially for financial
7 participation, as in the data. Thus, we find that wealth-constrained choices related
8 to occupation and financial participation are indeed significant channels at the
9 micro level that link growth and inequality dynamics at the macro level. This
10 confirms the existence of an intimate relationship between growth and inequality,
11 as Kuznets (1955) postulated. Here we identify occupational choice and financial
12 sector participation as sources of the relationship.

13 Differential growth rates across subgroups is another channel linking growth
14 and inequality at the aggregate level. In LEB, the income of the rich group,
15 entrepreneurs, declines over time because of the built-in diminishing returns,
16 whereas that of the poor group, workers, is increasing. Thus, positive within-group
17 growth comes only from the poor group. Income inequality eventually decreases
18 via this catchup effect. In contrast, in GJ, income grows faster in the rich group,
19 participants in the financial sector, than in the poor group, nonparticipants. The
20 income gap between two groups diverges. This is one of the main sources of
21 increasing inequality in GJ. Likewise, catchup growth is not captured by GJ. Poor
22 households either suffer low growth or graduate into the financial sector. In both
23 models, overall within-group growth is low relative to the data. There seem to be
24 some missing engines of growth within subgroups. Human capital is a candidate,
25 as identified by Jeong (2000).

26 Both models predict income gaps across key selection groups, which are far too
27 large. Thus, the orders of magnitude of the composition effects on income growth
28 and inequality change are exaggerated relative to the data. For the same reason, the
29 convergence effect in LEB and the divergence effect in GJ on inequality change are
30 also exaggerated. Each model has two kinds of heterogeneity: individual wealth
31 and random entrepreneurial talent in LEB and individual wealth and idiosyncratic
32 shocks for the risky investment in GJ. The assumed cross-sectional variation of
33 occupational choices or financial participation choices with wealth, when they are
34 forced onto the structure of the model, seem to require large counterfactual income
35 gaps.

36 Remarkably, the GJ model predicts well the overall shape of the income distribu-
37 tion at the end of the sample period. But both models do not predict well-observed
38 income variation in the upper and lower tails of income distribution. That is, for
39 upper tails, both models fail to predict the existence of extremely rich people. As
40 for the lower tail, the models fail in different ways. In LEB, wage earners and
41 subsisters are all alike, which creates a spike at the low end of income distribu-
42 tion and hence no income variation among poor people. In GJ, the poor group,
43 nonparticipants in financial sector, are subject to idiosyncratic shocks. There is
44 reasonable income variation among them, but the lower tail is strictly shifted to

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1 left, that is, there are too many poor people relative to the data. A mechanism is
2 needed in GJ under which poor people can escape poverty even when they are
3 outside the financial system. LEB with its increasing wages provides one such
4 mechanism.

5 There is also a noticeable discrepancy in subgroup inequality levels. In the
6 data, financial sector participant and nonparticipant groups have similar levels
7 of inequality. In GJ, the inequality level is much lower among participants than
8 among nonparticipants. But in LEB, the opposite is true. The low level of inequality
9 among participants in GJ suggests that financial sector is too good at diversifying
10 idiosyncratic shocks. Thus, we may need to make the insurance role of the financial
11 sector less than perfect. In LEB, the level of inequality is higher for participants
12 because of high interest rates (the return on saving amplifies wealth differences
13 into income differences), and because of high variation in wealth and talent for
14 participants (as low-wealth but high-talent households are not constrained in set-
15 ting up business in the financial sector but need to pay back interest). This suggests
16 that making the credit market less than perfect will improve subgroup inequality
17 dynamics. It is interesting that two quite distinct models suggest the common
18 necessity of less-than-perfect financial markets.

19 Indeed, one way to think about the model comparison exercise is to begin with
20 LEB, which has an exogenously expanding financial sector, and then compare
21 it to GJ with its endogenous costly entry. LEB is at loss to explain the higher
22 entrepreneurial income of financial sector participants, but GJ can reconcile that
23 anomaly. In effect, wealth constraints (entry cost) create rents, which shows up as
24 income differentials. Likewise, income growth among participant entrepreneurs is
25 anomalous in LEB, with its diminishing returns, but GJ with its Ak technology and
26 explicit modeling of information flows provides an explanation. Related also is
27 the diverging income levels between the participant group and the nonparticipant
28 group, not captured in LEB, but reconciled by GJ with its transaction cost.

29 By contrast, GJ leaves some open questions and anomalies of its own. GJ
30 captures endogenously the overall trend in financial sector participation but cannot
31 explain the relatively sharp upturn in participation after 1986. (The expansion was
32 imposed exogenously in LEB.) GJ is missing the catchup for nonparticipants, no
33 doubt because of missing the wage growth effect, which is picked up well by
34 LEB.

35 Both models fail to predict the close relationship between the growth patterns
36 of the entrepreneurs in financial sector (the smallest but richest group in the Thai
37 economy) and the aggregate movements of growth and inequality over time. GJ
38 simply does not distinguish occupations. LEB does feature occupations, but the
39 entrepreneurs *in* the financial sector are predicted to have diminishing income
40 growth. Furthermore, the income of entrepreneurs outside the financial sector in-
41 creased after 1992 even as income growth of entrepreneurs in the financial sector
42 declined. That is, in the data, entrepreneurs seem to face different kinds of technol-
43 ogy and shocks, depending whether or not they participate in the financial sector.
44 Part of the decrease in inequality after 1992 is related to the differential income

1 growth between the participant entrepreneurs and nonparticipant entrepreneurs.
2 These phenomena should not be ignored in future work.

3 Many of these failures seem to be related to insufficient heterogeneity and overly
4 simplistic model structures. A remedy might be to introduce more heterogeneity
5 and additional features of various kinds. That is, it is tempting to think that all
6 one needs to do is to make the models more realistic by adding more kinds of
7 heterogeneity. However, we have learned from the model comparison exercise of
8 this paper that additional heterogeneity *per se* does not necessarily help to improve
9 dynamics or cross-sectional income variation. LEB has more key categories than
10 GJ, and LEB is forced to replicate the financial sector expansion in the data.
11 However, LEB does worse in predicting distributional shapes, subgroup inequality
12 dynamics (e.g., virtually no inequality among non-participants), and income gaps
13 across subgroups. Thus, the compositional effects and convergence/divergence
14 effects are more at odds with the data in LEB than in GJ.

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3. LEB MODEL

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3.1. Model Economy

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We first consider a model of occupational choice, constrained by wealth because
of the presumed lack of a credit market as in Lloyd-Ellis and Bernhardt (2000).
The economy is populated by a continuum of agents of measure one evolving
over discrete time $t = 0, 1, 2 \dots$. An agent with end-of-period wealth W_t at date t
maximizes individual preferences over consumption c_t and wealth carry-over b_{t+1}
as represented by the utility function:

26

27

$$u(c_t, b_{t+1}) = c_t^{1-\sigma} b_{t+1}^\sigma,$$

28

29

subject to the budget constraint $c_t + b_{t+1} = W_t$.

30

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There are two kinds of production technologies. In traditional sector, everyone
earns a safe subsistence return γ of a single-consumption good. In the modern
sector, entrepreneurs hire capital k_t and labor l_t at each date t to produce the
single-consumption good according to a production function:

34

35

$$f(k_t, l_t) = \alpha k_t - \frac{\beta}{2} k_t^2 + \xi l_t - \frac{\rho}{2} l_t^2 + \sigma l_t k_t.$$

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Each worker provides a single unit of time and is paid by wage w_t at date t . The
cost of capital is determined by its opportunity cost, a constant interest rate of
unity tied to a backyard technology. There is a fixed cost of entry into business in
the modern sector. That is, the entrepreneur pays an initial setup cost x_t to start
up a business. The setup cost represents the inverse of the innate entrepreneurial
talent of each agent, and it is assumed to be independent of the wealth level b_t and
randomly drawn from a time invariant cumulative distribution:

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$$H(x) = mx^2 + (1 - m)x. \quad (1)$$

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1 The support of x is unit interval $[0, 1]$ and the range of possible values for parameter
 2 m is $[-1, 1]$. This class of distributions subsumes the uniform distribution at
 3 $m = 0$. As m increases toward 1, the distribution of x becomes more skewed to
 4 the right and, hence, efficient entrepreneurs become rare.

5 In this model, an agent is distinguished by a pair of beginning-of-period char-
 6 acteristics: initial wealth b and randomly drawn entrepreneurial (lack of) talent
 7 x , where we suppress the time subscript on these to emphasize the recurrent or
 8 stationary aspect. With the above utility function, the optimal rules for consump-
 9 tion and saving will be linear functions of wealth, and so preference maximization
 10 is equivalent to end-of-period wealth maximization. Thus, given an equilibrium
 11 wage rate w , an agent of type (b, x) chooses his occupation to maximize his total
 12 wealth W :

$$\begin{aligned} 13 & \\ 14 & W = \gamma + b, \quad \text{for subsisters} \\ 15 & \quad = w + b, \quad \text{for wage earners} \\ 16 & \\ 17 & \quad = \pi(b, x, w) + b, \quad \text{for entrepreneurs,} \end{aligned} \quad (2)$$

18 where
 19

$$20 \quad \pi(b, x, w) = \max_{k,l} \{f(k, l) - wl - k - x\} \quad \text{subject to} \quad (3)$$

$$21 \quad 0 \leq k \leq b - x. \quad (4)$$

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 25 Equation (2) suggests that there is a reservation wage level $\underline{w} = \gamma$ below which
 26 every potential worker prefers to remain in subsistence sector. Likewise, if the
 27 wage rate exceeds that reservation wage, no one remains in subsistence sector.
 28 Therefore, the model implies that wage must be $\underline{w} = \gamma$ when the subsistence
 29 sector coexists with the modern sector. We allow the subsistence income γ to
 30 grow exogenously at the rate of g_γ . As long as two sectors coexist, the demand
 31 for labor from the modern sector determines the population proportions of wage
 32 earners and subsisters.

33 The higher is the initial wealth b , the more likely it is that an agent will be
 34 an entrepreneur. A potentially efficient, low x , agent may end up being a worker,
 35 constrained by low initial wealth b . Given wealth b and market wage w , we
 36 can define a marginal agent as one with setup cost $x^m(b, w)$ who is indifferent
 37 between being a worker and being an entrepreneur such that $\pi(b, x^m, w) = w$. If
 38 the randomly assigned setup cost is higher than this setup cost, the household will
 39 be a worker for sure. However, with the constraints on capital demand in (4), the
 40 setup cost x cannot exceed the own wealth b either. Therefore, given wage w , the
 41 critical setup cost for the marginal agent with wealth b , who is willing to be an
 42 entrepreneur, is characterized by

$$43 \quad z(b, w) = \min[b, x^m(b, w)]. \quad (5)$$

44

1 This is the key selection equation, which will be used later in estimating the
2 parameters of the LEB model.

3 In sum, households of varying talent face imperfect credit markets in financing
4 the establishment of modern business and in expanding the scale of enterprise.
5 Thus, households are constrained by limited wealth on an extensive margin of
6 occupational choice and intensive margin of capital utilized, although both con-
7 straints can be alleviated over time. As the distribution of wealth evolves, so does
8 the occupational composition of population and income differentials, generating
9 the dynamics of growth with changing inequality.

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3.2. Estimation

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3.2.1. *Likelihood function.* Wealth-constrained occupational choice is the key building block or micro foundation of the LEB model, and the mapping from wealth to occupation itself is stationary, conditional on wage w . Thus, we form a likelihood function of occupational choice as is implied by the theory, and then estimate the key parameters by maximizing the likelihood of the micro data. Because households will at best be indifferent between being wage earners and being subsisters, the crucial occupational choice is binary, between being an entrepreneur or not.

Let y_i denote the binary occupational choice of agent i that assigns 1 for being an entrepreneur and 0 otherwise. Then, given wage w , the probability of being an entrepreneur for agent i with wealth b_i is given by

$$\Pr\{y_i = 1\} = \Pr(x_i \leq z(b_i, w)), \quad (6)$$

where z is the critical setup cost function, defined in (5).⁵ Then, given the profiles of occupational choice and initial wealth $(y_i, b_i)_{i=1}^n$ of n households in cross-section data, the log likelihood function is written:

$$\log L = \sum_{i=1}^n \{y_i \ln[\Pr(x_i \leq z(b_i, w))] + (1 - y_i) \ln[1 - \Pr(x_i \leq z(b_i, w))]\}, \quad (7)$$

where

$$\Pr(x_i \leq z(b_i, w)) = mz(b_i, w)^2 + (1 - m)z(b_i, w), \quad (8)$$

from the time-invariant distribution of random setup cost x , specified in (1).

The critical setup cost function $z(b, w)$ is determined by the optimal profit function in (3) and, hence, by the production technology parameters $(\alpha, \beta, \xi, \rho, \sigma)$. Used also in equation (8) is the parameter m of the talent distribution H . We can thus apply maximum likelihood methods, taking the log likelihood function in (7) to the data on occupational choice in the real Thai economy, to estimate the parameters of technology and distribution of the random talent (setup cost). We may interpret the chosen parameters from this estimation as those that best fit the micro foundation of the LEB model.

1 Two things are to be mentioned about the estimation. First, because of the
 2 quadratic form of technology, the optimal profit function can be written as a
 3 reduced-form second-degree polynomial in capital and, hence, only three out of
 4 five technology parameters can be identified if we use a single wage. However, by
 5 varying the wage over initial time periods in relation to the exogenous parameter
 6 of subsistence income γ , we can solve this identification problem. The details of
 7 identification are discussed in Appendix A.2. Second, not all remaining parameters
 8 can be estimated. The subsistence income level γ and the preference parameter
 9 ϖ , the marginal propensity to save, are not directly related to occupational
 10 choice and cannot be identified from this estimation. Both ϖ and γ are calibrated
 11 below.

12
 13 *3.2.2. Estimates.* We estimate and simulate the model using the Thai Socio-
 14 Economic Survey (SES), a nationally representative household survey in Thailand
 15 for the two decades between 1976 and 1996. The economically active house-
 16 holds in the SES data are used. More details of the SES data are described in
 17 Appendix A.1.

18 In order to estimate the mapping between *initial* wealth and *subsequent* oc-
 19 cupational choice, as the model suggests, we use only the sample of “young”
 20 households whose heads’ age is below 30.⁶ The choice of cutoff age for “young”
 21 households depends on how closely their *current* wealth approximates their *initial*
 22 wealth because there is a possibility of wealth accumulation over time, even in the
 23 early careers of young households. Thus we compare the cohort age profiles of
 24 wealth between the young household group (age < 30) and the rest (age \geq 30),
 25 plotted in Figures A.1 and A.2. We can see that the age profiles of wealth of the
 26 young households are literally flat or at least much flatter than those of older ones.
 27 Figures A.3 and A.4 compare the age profiles of wealth for entrepreneurs only.
 28 Reassuringly, the age profiles of wealth of the young entrepreneurs are flatter than
 29 those of older ones, except the latest cohort. Thus, in the data, young entrepreneurs
 30 do not accumulate wealth at a high rate so that the current wealth we observe would
 31 be close to initial wealth.

32 The likelihood function in (7) is written for the benchmark LEB model without
 33 credit and so we exclude households who participate in the financial sector, to
 34 make consistent use of data in estimation. We also use the wage variation only at
 35 the initial two years, 1976 and 1981, during which the Thai wage is considered to
 36 be close to the reservation wage that grows exogenously in the model.

37 There is an additional parameter implicitly involved in estimation, the *scale* that
 38 converts wealth in the data (in Thai baht unit) into wealth in the LEB model. The
 39 choice of the scale is important because the random setup cost x is specified with
 40 bounded support $[0, 1]$, and enters in the model in an additive way. We take this
 41 scale to be a free parameter and calibrate it as $6 * 10^{-8}$. The way we calibrate the
 42 scale will be discussed in the next subsection.

43 Table 1 reports the estimated parameter values from the maximum likeli-
 44 hood estimation.⁷ The average value of log likelihood is -0.4898 . The bootstrap

TABLE 1. Estimated LEB parameters

α	β	ξ	ρ	σ	m
1.0011	0.0940	0.0566	0.0033	0	-1
(0.2559)	(0.0103)	(0.0007)	(0.0000)	(0.0001)	(0.0000)

standard errors of the estimates are reported in parentheses.⁸ The standard errors are all small and the parameters are fairly precisely estimated.

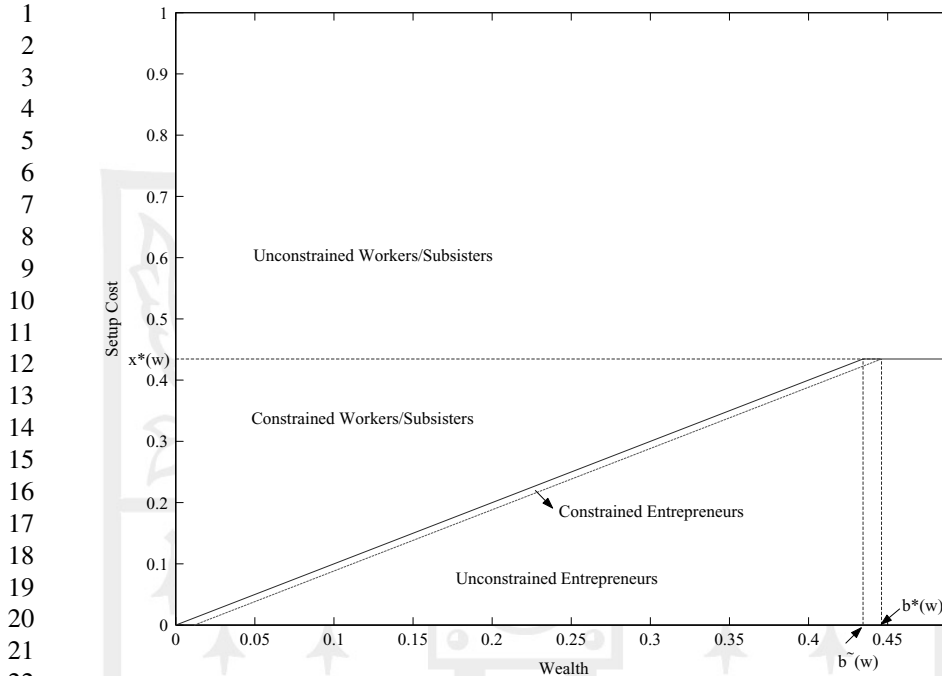
The LEB model implies an occupational map that partitions the type space (b, x) into four areas: (1) an area of unconstrained subsisters and wageworkers (whose fixed costs are too high, higher than some critical level $x^*(w)$, for them to be entrepreneurs regardless of wealth levels); (2) an area of constrained subsisters and wageworkers (whose fixed costs are lower than $x^*(w)$ but their wealth levels are not high enough to self-finance the fixed costs to be entrepreneurs); (3) an area of constrained entrepreneurs (whose fixed costs are low enough and wealth levels high enough to cover the fixed costs, but not sufficient to finance the unconstrained level of working capital); (4) and an area of unconstrained entrepreneurs (whose wealth levels are sufficient, higher than a critical level $b^*(w)$, to cover both their fixed costs and the unconstrained level of working capital). Let $\tilde{b}(w)$ be the wealth level below which the wealth constraint binds exactly at the level of setup cost ($x = b$) and, hence, the capital demand k hits the lower bound at zero. The three parameters $x^*(w)$, $b^*(w)$ and $\tilde{b}(w)$ determine the shape of the occupational map, conditional on a given wage w .⁹ The occupational map at 1976 wage at the above estimates is displayed in Figure 1.

3.3. Calibration

As was mentioned earlier, the wealth scale is a free parameter and estimation is defined conditional on the scale. This is the key parameter that generates a trade-off between cross-sectional estimation and dynamic simulation. We find that the estimated fractions of entrepreneurs in the LEB parameter space are always lower than those in the data, but the higher the scale is, that is, the wealthier the LEB economy becomes, the higher is the likelihood of estimating the cross-sectional occupational choice. But more wealth makes the LEB agents consume their wealth rather than save it and the economy suffers from negative growth initially.¹⁰ The higher the scale, the more negative is this initial negative growth. Although this relationship is not monotone, and eventually the economy starts to grow, as in the data, overall growth for the entire sampling period can be negative when the initial negative growth is too large. So we restrict our search for scale parameter such that this does not happen. The set of estimates reported in Table 1 is the one with the highest likelihood within this range of scales.

The subsistence income γ , its exogenous growth rate g_γ , and the preference parameter ϖ are not related to the occupational choice and they cannot be

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23 **FIGURE 1.** Estimated LEB occupation map.

24
25 determined from the above estimation. The subsistence income γ is calibrated
26 at 0.012 to match the initial average wage income in 1976, given the above chosen
27 scale. This calibration is equivalent to assuming that the 1976 wage in Thailand is
28 close to the reservation wage. We allow this reservation wage to grow exogenously
29 at the rate of 0.5 percent per year, which matches the annual average growth rate
30 of wage income during the first decade 1976–1986. The wage income in Thailand
31 surged only after 1986 and we consider that the wage growth before 1986 is a result
32 of exogenous growth of reservation wage. The Cobb-Douglas form of preferences
33 implies that ϖ can be interpreted as a savings rate. Thus, we calibrate ϖ at 0.25,
34 matching the average saving rate (with standard error of 0.0204) from the SES
35 during the 1976–1996 period. Thus, all free parameters are calibrated from the
36 same SES data that are used for estimation.

37
38
39 **3.4. Evaluation**

40 *3.4.1. Aggregate dynamics.* The simulated aggregate dynamics paths of LEB
41 are compared with those in the Thai data in Figure 2.¹¹ The model does capture
42 the overall growth and particularly the accelerated upturn in growth starting 1986
43 (Figure 2.2). The initial growth rate of the model is higher than the data, but it
44 quickly approaches the low rate of growth in the Thai data, near zero, before the

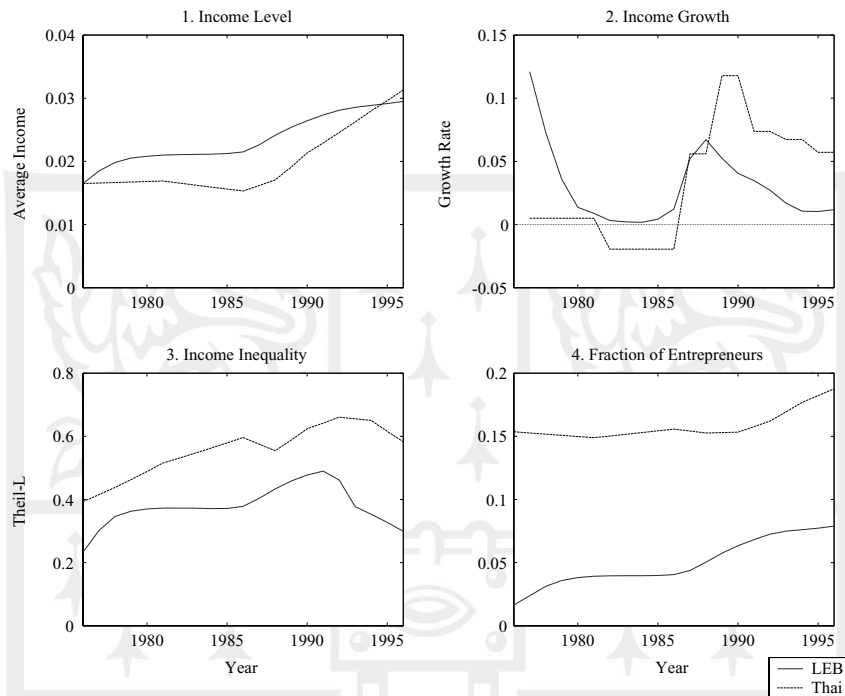


FIGURE 2. LEB aggregate dynamics.

upturn of late 1980s. Inequality dynamics, in particular the overall increase and eventual decrease beginning in early 1990s in Thailand, are also captured, but the predicted level of total inequality in the model is consistently lower than in the data (Figure 2.3). The fraction of entrepreneurs increases both in the model and the data (Figure 2.4). However, the model starts at a lower fraction of entrepreneurs and predicts a noticeable rise during the expansion of the financial sector after 1986, whereas the fraction rises a little later in the data, in 1990.

Evidently, LEB can capture both growth and inequality aggregate dynamics without aggregate shocks, but, as will be shown in the following sections, it does so through endogenous changes in factor prices, that is, wages and interest rates, and through endogenous occupational shifts. However, the exogenously embedded financial expansion is the force behind both the growth dynamics and population dynamics.

3.4.2. Population dynamics. We categorize the population into four subgroups, distinguishing both financial participation and occupation. In the legends in the Figures hereafter, “np” denotes nonparticipants in the financial sector, “p” participants in the financial sector, “e” entrepreneurs, and “ne” nonentrepreneurs. (Nonentrepreneurs include both workers and subsisters, but we will sometimes use

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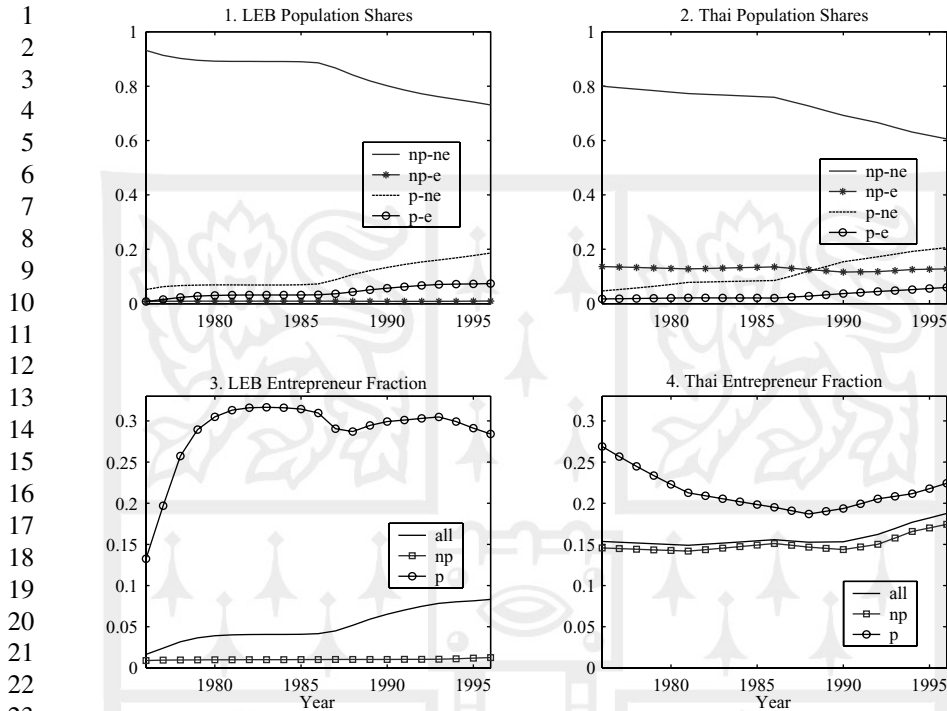


FIGURE 3. LEB population dynamics.

workers and nonentrepreneurs interchangeably because workers and subsisters are all alike in LEB.)

Population shares of the four subgroups are plotted in Figures 3.1 (LEB) and 3.2 (Thai). The directions of compositional change in the model agree with the data. The majority of households are the nonparticipant nonentrepreneurs, but their population share is declining over time in the model, as shown in the data. The population share of nonparticipant entrepreneurs is low and stable over time, as in the data. The population shares of participants of each occupation are increasing in both the model and the data. However, the smallest group are nonparticipant entrepreneurs in the model, whereas the participant entrepreneurs are the smallest group in the data.

The model predicts a larger fraction of entrepreneurs among participants than among nonparticipants, as in the data, although the difference is larger in the model than in the data (Figures 3.3 and 3.4). Except for an initial increase among participants, the fraction of entrepreneurs is more or less stable in the model, among both participants and nonparticipants in the model. Thus, the increase of the economy-wide population share of entrepreneurs is a result of the expansion of financial sector, where there are more entrepreneurs.

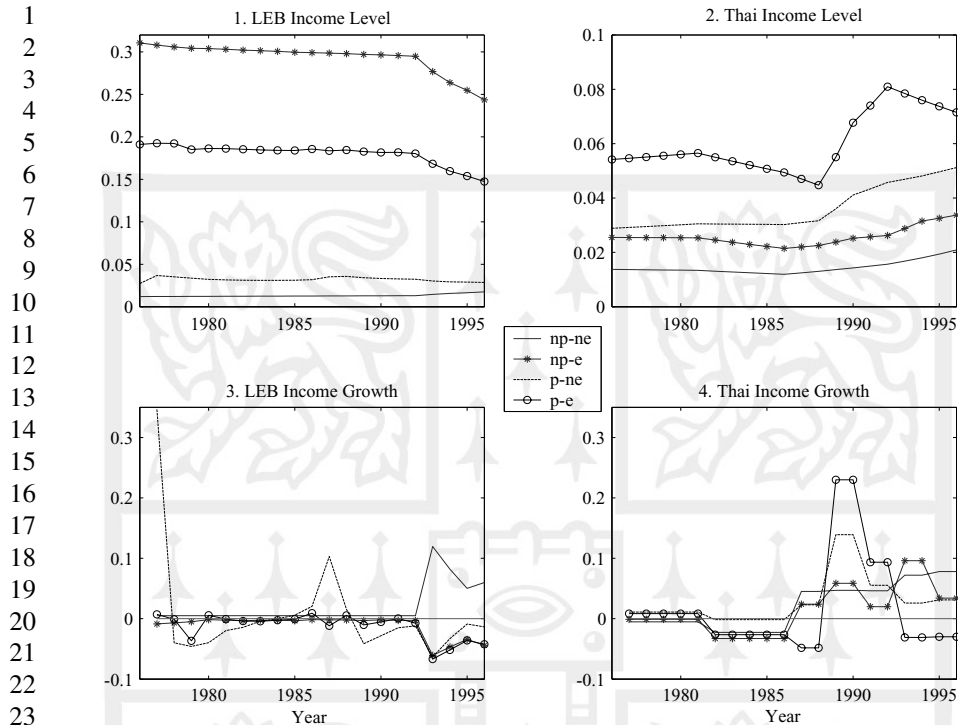


FIGURE 4. LEB subgroup growth dynamics.

3.4.3. *Subgroup dynamics.* The patterns of subgroup income levels in LEB are displayed in Figure 4.1, juxtaposed with the Thai data in Figure 4.2. Entrepreneurs earn higher income than nonentrepreneurs either within or outside of the financial sector, also true in the data. The richest group in the model are nonparticipating entrepreneurs. However, the richest in the data are *participant entrepreneurs*. In fact, nonparticipating entrepreneurs are poorer than participant workers in the data. Thus, nonparticipating entrepreneurs in the model are too rich. With no access to credit, only the very wealthy can become entrepreneurs to self-finance both the setup cost and the capital. Talented but poor people may not become entrepreneurs if they are outside the credit sector. In contrast, in the credit sector, the poor can be entrepreneurs if their setup cost is low enough. But talented poor people who borrow in the credit sector need to pay the loan back with interest, leaving them poorer in net income than the nonparticipating entrepreneurs who self-finance. (Note that entrepreneurs in both sectors do share the common wage as well as technology.) Thus, on average, entrepreneurial income is higher among non-participants than among participants in the model. (The reverse is true in the data.) We may interpret this entrepreneurial income differential of the model as a “rent” due to the imposed factor market structure, that is, a segmented capital market but with an integrated labor market.

1 In the model, the income of nonparticipant workers grows slowly but steadily
2 but the income of participant workers does not show any trend. In the data, the
3 increasing trend of income of workers is more salient for both participants and
4 nonparticipants. Entrepreneurial income continually decreases over time among
5 both participant and nonparticipant groups in the model, as a result of the di-
6 minishing returns to capital in the LEB technology. This decline is accelerated
7 after the wage starts to grow endogenously in 1991. In the data, entrepreneurial
8 incomes also decline for both participants and nonparticipants for the first decade.
9 But after 1986, the income of nonparticipant entrepreneurs steadily *increases*,
10 peaking after 1992. The income of entrepreneurs in the financial sector increases
11 greatly during 1988–1992, then decreases after 1992. Thus, the movements of
12 profits differ between participants and nonparticipants in the data. This suggests a
13 possibility that the participant group and the nonparticipant group may not share
14 a common technology in the data.

15 Observing the subgroup growth patterns in the data delivers us another inter-
16 esting point. Note that the period of accelerated income growth of the participant
17 entrepreneurs corresponds to the growth-peak period of aggregate income. Also
18 the point at which the income growth rate of this group begins to decrease corre-
19 sponds to the turning-point of the aggregate income inequality, from an increasing
20 to a decreasing trend. That is, in the data, the nonlinear dynamics of aggregate
21 income growth and aggregate inequality change are closely related to the growth
22 pattern of *entrepreneurs in the financial sector, the richest subgroup*, although
23 their population share is quite low, going from 2 to 6 percent over time. In LEB,
24 the patterns of entrepreneurial income growth are common between the partici-
25 pants and nonparticipants, that is, the continual decline of profits, because of the
26 common diminishing-return technology. Thus, LEB cannot capture the relation-
27 ship between the aggregate movement of income growth and inequality and the
28 income growth pattern of the *participant entrepreneurs* that is observed in the
29 data.

30 Income growth rates co-move in the data across occupation groups within the
31 financial sector (Figure 4.4). Although much less obvious, this co-movement exists
32 in the model, which is related to the movement of the interest rate and hence finan-
33 cial income (Figure 4.3). The co-movements of growth rates across occupation
34 groups among nonparticipants are weak, particularly in the model. In fact, the
35 growth rate of the nonparticipant workers is counter to that of nonparticipant
36 entrepreneurs during the period of endogenous wage growth in the model, and
37 this is also true in the data for the same reason toward the very end of the second
38 decade. However, the model does not capture the co-moving low growth rates
39 among nonparticipants for the first decade.

40 The entrepreneurial income premium is shown in Figure 5.1, in comparison
41 with the Thai data in Figure 5.2. The income premium of entrepreneurs over
42 wage earners decreases over time for both nonparticipants and participants in
43 the model, as in the data. The eventual decrease in aggregate inequality, shown
44

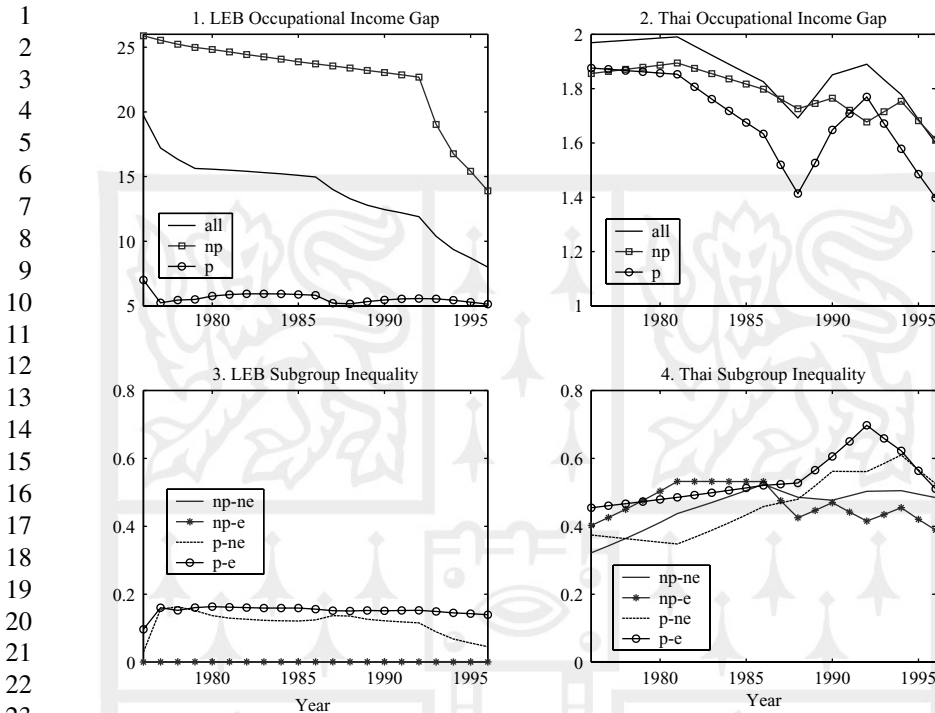


FIGURE 5. LEB subgroup inequality dynamics.

earlier in Figure 2.3, is mainly driven by (endogenous) wage growth and, hence, a decrease in the occupational income gap, as in the data. However, the income gaps are much larger, going from 26 to 13 among nonparticipants and from 7 to 5 among participants in the model than in the data, varying from 1.89 to 1.60 among nonparticipants, and from 1.88 to 1.40 among participants. These occupational income gap changes are mirror images of the above subgroup growth patterns, that is, the continual increase of wage income among the nonparticipant workers, the poorest group, and the continual decrease of profit income among the nonparticipant entrepreneurs, the richest group. This in fact is the source of decreasing aggregate inequality after 1992. Thus, the direction of the occupational income gap change over time agrees with the data, but there is a huge discrepancy in orders of magnitudes.

The model predicts a clear inequality ordering between participants versus non-participants, for each occupation, in Figure 5.3. Inequality levels are much higher among participants than among nonparticipants. In fact, there is literally no inequality among nonparticipant workers, and the inequality among nonparticipant entrepreneurs is virtually nil. The higher level of inequality among participants is due in part to interest income, amplifying wealth differences into income

1 differences, and in part due to more talent variation among entrepreneurs with ac-
 2 cess to credit. In the data, in Figure 5.4, the inequality-ordering across subgroups
 3 is less clear, except that income inequality of entrepreneurs in the financial sector
 4 is higher than workers in the financial sector. The Thai data show co-movements
 5 of inequality levels across occupation groups in the financial sector but this is
 6 weak in the model. Finally, the model predicts much lower subgroup inequality
 7 levels for all four groups than in the data. Income variation within every subgroup
 8 is too small in the model relative to the data.

9
 10 *3.4.4. Decomposition formulae.* Aggregate dynamics are generated from the
 11 above population dynamics and subgroup dynamics. We decompose the aggregate
 12 growth of mean income and income inequality into the contributions of those
 13 underlying components according to the following formulae.

14 The aggregate mean income μ is a sum of subgroup mean income μ^k 's, weighted
 15 by subgroup population shares p^k 's:

$$16 \quad 17 \quad 18 \quad 19 \quad \mu = \sum_{k=1}^K p^k \mu^k.$$

20 The change in mean income is thus decomposed into two parts, one from the
 21 changes in population shares Δp^k 's, and the other from growth within subgroups
 22 $\Delta \mu^k$'s:

$$23 \quad 24 \quad 25 \quad 26 \quad \Delta \mu = \sum_{k=1}^K \bar{p}^k \Delta \mu^k + \sum_{k=1}^K \bar{\mu}^k \Delta p^k, \quad (9)$$

27 where Δ denotes the difference over time and the upper bar the average over
 28 time. This is simply a discrete version of product rule, which can be applied to
 29 any additive indices. We will use the decomposition formula in terms of overall
 30 growth *rate*, by measuring changes between the beginning and ending points for
 31 two decades, dividing all terms in (9) by the initial mean income level.

32 Theil-L entropy index I , our measure of income inequality, is also additively
 33 decomposable into *within-group inequality* WI and *across-group inequality* AI
 34 as follows:

$$35 \quad 36 \quad I = WI + AI, \quad (10)$$

$$37 \quad 38 \quad 39 \quad 40 \quad WI = \sum_{k=1}^K p^k I^k, \quad AI = \sum_{k=1}^K p^k \log \left(\frac{\mu}{\mu^k} \right),$$

41 where I^k denotes the inequality within subgroup k . The within-group inequality
 42 WI is a sum of the subgroup inequality I^k 's weighted by the population shares
 43 of subgroups. The across-group inequality AI is a sum of log inverse of relative
 44 incomes, again weighted by the population shares of subgroups.

1 Because of the additive nature of the Theil-L index, we can also apply this
2 discrete product rule to the inequality change over time as follows:

$$3 \quad \Delta I = \Delta WI + \Delta AI, \quad (11)$$

$$4 \quad \Delta WI = \sum_k \bar{p}^k \Delta I^k + \sum_k \bar{I}^k \Delta p^k,$$

$$5 \quad \Delta AI \doteq \sum_k \left[\left(\frac{p^k \mu^k}{\mu} \right) - \bar{p}^k \right] \Delta \log \mu^k + \sum_k \left[\left(\frac{\mu^k}{\mu} \right) - \log \left(\frac{\mu^k}{\mu} \right) \right] \Delta p^k. \quad (12)$$

6
7
8 The change in total inequality is decomposed into the change in within-group
9 inequality ΔWI and the change in across-group inequality ΔAI .¹² The within-
10 group inequality change ΔWI is further decomposed into the change in subgroup
11 inequality and the change in population composition as in (12). The across-group
12 inequality change ΔAI is decomposed into two components as well: the change
13 in relative income gaps across subgroups, the first term in (12), and the change as
14 a result of the population composition changes, the second term in (12). Note that
15 $\Delta \log \mu^k$ approximates the growth rate of average income of subgroup k ; hence,
16 the first term in (12) captures the inequality change because of the differential
17 growth rates across subgroups weighted appropriately. When a higher-income
18 group grows faster than a lower-income group, the income gap between the two
19 diverges and the across-group inequality increases (or vice versa). We thus call this
20 term *divergence (or convergence) effect*. We will use the decomposition formulae
21 by normalizing the terms in (12) and (12) by the initial inequality level.

22
23
24
25
26 **3.4.5. Decomposition results.** The two-decade growth rate of mean income is
27 decomposed into the contributions of subgroup growth and compositional growth
28 for both the LEB model and the Thai data in Table 2, using the above formula
29 in (9). We partition the population: by occupation category only, by financial
30 participation only, and then by joint categories distinguishing both occupation and
31 financial participation.

32 The model almost matches the overall income growth rate (0.869 for LEB and
33 0.899 for Thailand). However, growth comes mainly from occupational shifts in
34 the model (at the rate of 0.754), but this composition effect on growth is small in the
35 data (at the rate of 0.032). Partitioning the population by financial participation and
36 ignoring the difference in occupation, the composition effect from the (exogenous)
37 expansion of intermediation contributes substantially to growth in the model (at the
38 rate of 0.456) as in the data (at the rate of 0.319). Distinguishing the population by
39 both occupation and financial participation, we observe in the model a magnitude
40 of composition effect similar to the case when only the occupation is distinguished.
41 This implies that the huge dominance of the composition effect on growth in the
42 model is mainly due to the enormous *occupational* income gaps (varying from 26
43 to 13 among nonparticipants and from 7 to 5 among participants) rather than the
44 income gap between financial participants and nonparticipants.

TABLE 2. Decomposition of aggregate income growth in LEB

By Occupation			
	Subgroup	Composition	Total
Thailand	0.867	0.032	0.899
LEB	0.115	0.754	0.869
By Financial Participation			
	Subgroup	Composition	Total
Thailand	0.580	0.319	0.899
LEB	0.413	0.456	0.869
By Joint Category			
	Subgroup	Composition	Total
Thailand	0.573	0.326	0.899
LEB	0.141	0.728	0.869

The total inequality level can be decomposed into within-group inequality and across-group inequality as in equation (10). This is displayed in Figure 6, for both LEB and Thailand, taking the population partition by joint categories. This suggests that across-group inequality is the main component of total inequality in the model while within-group inequality is the main one in the data.

The two-decade growth rate of total inequality is decomposed for both the model and the data in Table 3, using equations (12) and (12).¹³ The model predicts an overall increase in inequality at 0.338 but this is less than in the data at 0.483.

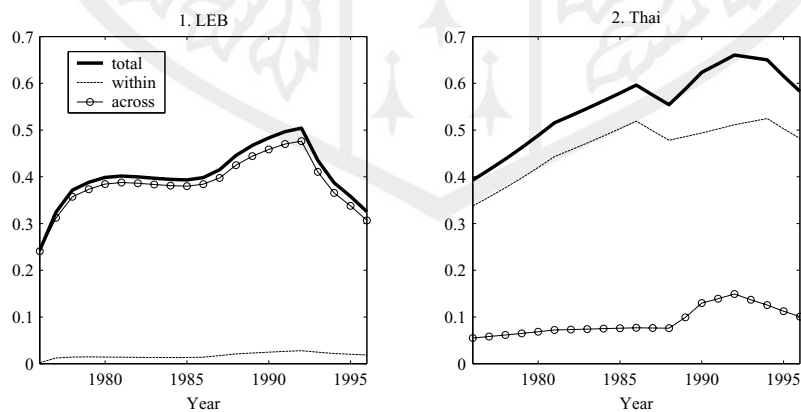
**FIGURE 6.** Within vs. across inequality decomposition.

TABLE 3. Decomposition of aggregate inequality change in LEB

By Occupation					
	Within-Group		Across-Group		Total
	Subgroup	Composition	Income Gap	Composition	
Thailand	0.524	0.001	-0.051	0.010	0.483
LEB	0.042	0.022	-1.056	1.881	0.338
By Financial Participation					
	Within-Group		Across-Group		Total
	Subgroup	Composition	Income Gap	Composition	
Thailand	0.304	0.032	0.015	0.133	0.483
LEB	-0.177	0.189	-0.066	0.439	0.338
By Joint Category					
	Within-Group		Across-Group		Total
	Subgroup	Composition	Income Gap	Composition	
Thailand	0.340	0.028	-0.003	0.120	0.483
LEB	0.015	0.053	-0.750	1.371	0.338

Distinguishing the population by occupation only, the model predicts an increase in subgroup inequality, a decrease in inequality through a converging occupational income gap, and an increase in inequality through the two composition effects. The directions of all these effects on inequality change in the model are consistent with the data. However, the orders of magnitudes of all these effects are quite different from the data. In the model, the subgroup inequality change is too small, and the convergence and composition effects are much too big.

Distinguishing the population by financial participation only, the model delivers a significant composition effect of financial expansion on across-group inequality, as in the data. However, subgroup inequality levels among both participants and non-participants decrease in the model, different from the data. This is because of the decrease in occupational income gap within each sector. Also, the model predicts convergence in income levels between participants and nonparticipants, but we observe divergence in the data. Thus, exogenous incorporation of financial expansion helps to explain the composition effects on inequality change (and income growth as well) but creates anomalies in other dimensions. We will see if endogenizing the financial participation decision can remove these anomalies in the LEB model. Distinguishing by both characteristics, the features of decomposition are similar to the decomposition by occupation only, but the difference in magnitudes between the model and the data becomes smaller.

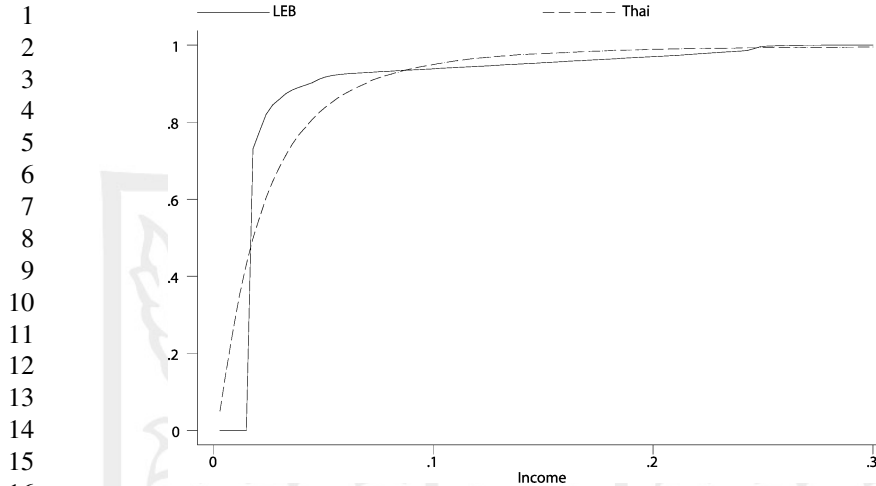


FIGURE 7. CDF of 1996 income distribution.

3.4.6. *End-of-sample-period income distribution.* The cumulative distribution functions of the income distributions at the end of sample period, 1996, are plotted for both the LEB model and the Thai data in Figure 7. The main discrepancy comes from the lower tail of the distribution. There is a spike at the low end of income distribution due to the common wage in the model, whereas there is much more income variation within the lower tail in the data. In the upper tail of the distribution, there is a slight bimodality in the model due to the income gap between nonparticipant entrepreneurs and participant entrepreneurs, and there are no extremely rich people that are present in the data. Thus, the model does not capture the income variation at both lower and upper tails in the data.

We formally test the goodness of fit of the end-of-sample-period income distribution of LEB relative to the Thai data. The income distribution in the data is not necessarily close to some *a priori* parametric form. The income distributions from the model are endogenously determined, evolving over time and would be distorted by imposing parametric forms on them. Thus, we compare distributional shapes between the model and the data in a *nonparametric* way, using the Kolmogorov-Smirnov (KS) statistic:

$$KS = \sqrt{mn/(m+n)} \sup_{-\infty < y < \infty} |F_n(y) - G_m(y)|, \quad (13)$$

where G_m and F_n denote the empirical distribution functions from the model and the data, respectively, and m and n denote the sample size of the empirical distributions from the model and the data, respectively. The limiting distribution of this statistic is described in Smirnov (1948). The KS statistic for the LEB model is 3.04 and the corresponding p-value is less than 0.0000, strongly rejecting

1 similarity of income distributions between the LEB model and the Thai data.¹⁴
 2 This rejection is obviously due to the spike at the low end of the LEB distribution.

3.5. Sensitivity Analysis

6 We perform a sensitivity analysis for the LEB model, to check the robustness of our
 7 evaluation results. For the *estimated* parameters such as technology parameters
 8 ($\alpha, \beta, \xi, \rho, \sigma$) and talent distribution parameter m , an obvious concern would
 9 be sampling errors around the point estimates. However, the bootstrap standard
 10 errors of these estimates are small, virtually zero. In fact, varying the estimated
 11 parameters within the range of one or two standard-error bounds does not change
 12 the simulation results. Thus we further vary the parameter values within a 10-
 13 percent-deviation range.

14 The simulated dynamics for both growth and inequality turn out to be robust to
 15 parameters α, β , and σ , but sensitive to ξ and ρ .¹⁵ Explicit consideration of the
 16 profit function of LEB helps us to understand why. Given the quadratic production
 17 function, the profit function can be written

$$18 \quad \pi = C_0(w) + C_1(w)k + C_2k^2 - x, \quad (14)$$

19 where

$$22 \quad C_0(w) = \frac{(\xi - w)^2}{2\rho}, \quad (15)$$

$$24 \quad C_1(w) = \alpha - 1 + \frac{\sigma(\xi - w)}{\rho}, \quad (16)$$

$$27 \quad C_2 = \frac{1}{2} \left(\frac{\sigma^2}{\rho} - \beta \right). \quad (17)$$

28 Thus, three coefficients, $C_0(w)$, $C_1(w)$, and C_2 , determine the dynamics of profit
 29 growth in relation to wage w . These also determine the three occupational map
 30 parameters, $b^*(w)$, $x^*(w)$, and $\tilde{b}(w)$ ¹⁶ :

$$33 \quad \tilde{b}(w) = C_0(w) - w, \quad (18)$$

$$35 \quad x^*(w) = \tilde{b}(w) - \frac{C_1(w)^2}{4C_2}, \quad (19)$$

$$37 \quad b^*(w) = x^*(w) - \frac{C_1(w)}{2C_2}. \quad (20)$$

38 At our estimate of σ at zero, $C_1(= \alpha - 1)$ and $C_2(= -\frac{2}{\beta})$ are time-invariant and
 39 independent from the wage. Thus changes in α and β affect the shape of the profit
 40 function, and subsequently the income dynamics, but not in relation to the wage
 41 evolution. Changes in α and β affect x^* and b^* , again not in relation to the wage,
 42 with σ at zero. Thus, these changes do not shift the occupational map over time.
 43
 44

1 Varying σ away from zero, a change in α could affect income and occupational
 2 choice in relation to wage via $C_1(w)$. However, a range of σ of $[0, 0.013]$ turns out
 3 to be not wide enough to generate any significant changes. Figure A.7 shows that
 4 an increase in α to 1.3 (maximum allowable value) reduces the annual average
 5 income growth rate from 3.18% to 2.95%, and also reduces the annual average rate
 6 of increase in inequality from 1.47% to 0.80%. Occupation transition dynamics
 7 remain virtually the same.

8 By contrast, ξ and ρ can directly affect both income dynamics and occupational
 9 choice via $C_0(w)$ in relation to wage although σ is near zero. An increase in ξ
 10 implies an increase in the intercept term $C_0(w)$ of the profit function. It also implies
 11 an increase in marginal productivity of labor by constant term ($MPL = \xi - \rho l$ with
 12 σ at zero). This makes the modern business more profitable and draws more savings
 13 into the more productive modern business sector. Thus income growth becomes
 14 faster. However, its implication for inequality is a bit complicated. When wage
 15 is set at the reservation level, the benefits from an increase in labor productivity
 16 belong to entrepreneurs but not to workers, and inequality rises. Once the wage
 17 starts to grow endogenously, the increase in marginal productivity from an increase
 18 in ξ benefits workers. But because both ξ and w increase, the net effect on $C_0(w)$
 19 and on profits is not certain. An increase in ρ plays a similar role to a decrease
 20 in ξ . Figure A.8 displays that an increase in ξ by 10 percent to 0.0623 increases
 21 the annual average income growth rate from 3.18% to 3.49%, but makes income
 22 inequality decline so fast in the end that the overall annual average rate of inequality
 23 change becomes negative, to -2.8% . However, the *patterns* of dynamics still
 24 remain the same: income grows slowly for the first decade and then surges after
 25 the financial expansion; income inequality follows an inverted-U shaped path, and
 26 the declining inequality is as a result of the endogenous wage growth. Occupation
 27 transition dynamics are again robust to this change.

28 An increase in m decreases the population of talented people and income growth
 29 becomes slower. This also reduces the income gap between entrepreneurs and
 30 wage earners, hence the inequality level decreases. An increase in γ makes the
 31 economy richer and reduces the occupational income gap. But this is a level effect.
 32 In contrast, an increase in g_γ has no level effects but does have exogenous growth
 33 effects. An increase in ω induces higher saving. This makes wealth accumulation
 34 faster and the occupational transition easier for the constrained workers. Thus
 35 income grows faster and inequality starts to decline earlier. However, the orders
 36 of magnitude of the changes in aggregate dynamics from perturbing parameters
 37 m , γ , g_γ , and ω within 10-percent-deviation bands are small.
 38
 39

40 4. GJ MODEL

41 4.1. Model Economy

42
 43 In Greenwood and Jovanovic (1990), hereafter denoted by GJ, growth and the
 44 evolution of the income distribution are related explicitly to financial deepening,

1 that is, increasing participation in the financial sector. There exists a fixed entry
2 cost that endogenously constrains the participation decision.

3 Consider an economy with a continuum of agents on the unit interval $[0,1]$. They
4 live for an infinite, discrete number of periods $t = 0, 1, 2 \dots$. For every agent
5 j , there are two technologies available that can convert the capital investment i_{jt}
6 at date t into income $y_{j,t+1}$ at next date $t + 1$. One technology yields a safe but
7 relatively low rate of return δ per unit capital and the other gives a risky rate of
8 return $(\zeta_{t+1} + \epsilon_{j,t+1})$ with higher expected value, where ζ_{t+1} represents a common
9 aggregate shock and $\epsilon_{j,t+1}$ an idiosyncratic shock specific to agent j . The aggregate
10 shock ζ_{t+1} is governed by a time-invariant uniform distribution with support
11 $[\underline{\zeta}, \bar{\zeta}]$, and the idiosyncratic shock $\epsilon_{j,t+1}$ is governed by a time-invariant uniform
12 distribution with support $[-\bar{\epsilon}, \bar{\epsilon}]$ with $E(\epsilon_{j,t+1}) = 0$. Let $\eta_{j,t+1} = \zeta_{t+1} + \epsilon_{j,t+1}$
13 be the composite shock and Ψ^η be its cumulative distribution function. GJ assume
14 that the lower bound for the composite shock is positive, i.e., $\underline{\zeta} - \bar{\epsilon} > 0$.

15 Each agent j decides on running either technologies, with portfolio share ϕ_{jt}
16 for the risky one, at date t so that the next period beginning-of-period wealth $k_{j,t+1}$
17 can be written such as

$$18 \quad k_{j,t+1} = [\phi_{jt}\eta_{j,t+1} + (1 - \phi_{jt})\delta]i_{jt}. \quad (21)$$

19 He allocates his beginning-of-period wealth k_{jt} into current consumption c_{jt} and
20 capital investment i_{jt} , namely, $k_{jt} = c_{jt} + i_{jt}$. The objective is then to maximize
21 the discounted life-time utility stream:

$$22 \quad E \sum_{t=0}^{\infty} \beta^t \frac{c_{jt}^{1-\sigma}}{1-\sigma},$$

23 subject to the sequence of resource constraints of $k_{jt} = c_{jt} + i_{jt}$ and the law of
24 motion in (21).¹⁷ Agents are heterogeneous in their wealth levels in each period
25 for two reasons: first, the initial endowment k_0 at date 0 differs across agents,
26 distributed under a cumulative distribution function Λ_0 . Second, the history of
27 realizations of random shock up to date t $\{\epsilon_{j,s}\}_{s=0}^t$ differs across agents j 's.

28 Other than physical production, there is another "technology" available, namely,
29 *financial intermediation*. An intermediary can run a countable number of trials
30 for the risky technology and get advanced information on next period's return to
31 the risky project. Then, the intermediary invests in the risky project only if this
32 return exceeds the safe return δ . Furthermore, the intermediary can diversify the
33 idiosyncratic shocks $\epsilon_{j,t+1}$ by pooling participants' returns. It can pay back at date
34 $t + 1$ a promised return $r(\zeta_{t+1})$, to be spelled out below in (25), per unit of capital
35 invested at time t contingent on the realized aggregate shock ζ_{t+1} . Therefore, every
36 agent has an incentive to join the coalition of financial intermediaries.

37 There are key restrictions on the parameter space to make the above economy
38 work properly.¹⁸ In order to ensure the benefits of intermediation and the incentive
39 to invest positive amount in the risky production every period, we need to assume
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1 the following condition:

$$2 \quad E\{r(\zeta_{t+1})\} > E\{\zeta_{t+1}\} > \delta. \quad (22)$$

3
4 To avoid the economy from shrinking to negative infinity, we need:

$$5 \quad \delta > 1/\beta. \quad (23)$$

6
7 With the linear production technology, unbounded growth is possible in this model,
8 and in order to prevent the economy from exploding to infinity in utility terms, we
9 need

$$10 \quad \beta E\{r(\zeta_{t+1})^{1-\sigma}\} < 1. \quad (24)$$

11 These intermediary trading arrangements are costly, as in Townsend (1978).
12 There is an initial fixed cost α of admitting each participant into the financial
13 coalition and a variable cost of $(1 - \gamma)$ in proportion to the amount of funds each
14 agent invests in the coalition. Thus, the intermediary charges a lump sum entry fee
15 q for each participant in exchange for the rights to operate an individual's project.
16 The zero-profit condition for the intermediary implies

$$17 \quad r(\zeta_{t+1}) = \gamma \max\{\delta, \zeta_{t+1}\}, \quad (25)$$

$$18 \quad q = \alpha. \quad (26)$$

19
20 Given these entry and proportional fees, not everyone immediately joins the finan-
21 cial system. Only agents whose wealth levels exceed some critical level are willing
22 to join. That is, the choice of participation in the financial sector is constrained by
23 wealth.

24 The decision making of households can be characterized by a pair of value
25 functions: v^0 , the value function of nonparticipants, and v^1 , the value function
26 of participants. An agent j with wealth k_{jt} at date t who currently is not in the
27 intermediation coalition chooses the total investment i_{jt} and the portfolio ϕ_{jt}
28 between safe and risky projects according to the following functional equation:
29

$$30 \quad v^0(k_{jt}) = \max_{i_{jt}, \phi_{jt}} \{u(k_{jt} - i_{jt})$$

$$31 \quad + \beta E_{\eta_{j,t+1}} \max [v^0(k_{j,t+1}), v^1(k_{j,t+1} - q)]\} \quad \text{subject to (21),} \quad (27)$$

32 where $E_{\eta_{j,t+1}}$ is the expectation with respect to the composite shock $\eta_{j,t+1}$. An
33 agent who is already in the financial system decides only on total investment by
34 solving the following functional equation:

$$35 \quad v^1(k_{jt}) = \max_{i_{jt}} \{u(k_{jt} - i_{jt})$$

$$36 \quad + \beta E_{\zeta_{t+1}} v^1(k_{j,t+1})\} \quad \text{subject to } k_{j,t+1} = r(\zeta_{t+1})i_{jt}. \quad (28)$$

37 Note that the expectation operator in the participant's value function is taken
38 only with respect to the aggregate shock ζ_{t+1} because the idiosyncratic shock is
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1 diversified away. Also note that participants do not choose the portfolio between
 2 safe and risky investments because this decision is delegated to the intermediary
 3 who has advanced information on the aggregate shock. There is no value function
 4 for non-participants v^0 in (28) because $v^1(k) > v^0(k)$ for every k , so once an agent
 5 enters the intermediated sector, he will never exit.

6 In sum, households face wealth constraints in their decisions to undertake costly
 7 entry into the financial system itself. Participation in financial intermediaries
 8 provides the benefits of enhanced risk sharing and advanced information. As
 9 economy-wide wealth shifts to the right, more households gain access to financial
 10 intermediaries, and this changes the composition of income-status groups and the
 11 income gap across them, which in turn over time affects growth and inequality
 12 dynamics.

14 4.2. Estimation

15
 16 *4.2.1. Likelihood function.* Financial participation constrained by wealth is
 17 the key micro foundation of the GJ model. We form a likelihood function for the
 18 financial participation decision using the pair of dynamic programs in (27) and
 19 (28). Let d_{jt} denote the participation decision of agent j at date t , which assigns
 20 1 if agent j decides to participate in the financial sector, and 0 otherwise:

$$21 \quad d_{jt} = 1, \quad \text{if } v^1(k_{jt} - q) \geq v^0(k_{jt}) \\ 22 \quad \quad \quad = 0, \quad \text{if } v^1(k_{jt} - q) < v^0(k_{jt}). \quad (29)$$

23
 24 Townsend and Ueda (2006) show that there exists a unique critical value k^* such
 25 that the participation decision in (29) is equivalent to

$$26 \quad d_{jt} = 1, \quad \text{if } k_{jt} \geq k^* \\ 27 \quad \quad \quad = 0, \quad \text{if } k_{jt} < k^*. \quad (30)$$

28
 29 There is no closed-form solution for k^* because there are no analytic solutions
 30 to the dynamic program in (27). However, from the formulation of the dynamic
 31 programs in (27) and (28), it is clear that k^* is a function of the underlying
 32 parameters of the GJ model, $\theta^{GJ} = (q, \delta, \beta, \sigma, \gamma, \zeta, \bar{\zeta}, \bar{\epsilon})$,

$$33 \quad k^* = k^*(\theta^{GJ}).$$

34
 35 From the recursive nature of the above dynamic programming problems, the
 36 policy functions for portfolio and investment are time-invariant and depend on
 37 current wealth and the underlying parameters θ^{GJ} , that is, $\phi_{jt} = \phi(k_{jt}, \theta^{GJ})$ and
 38 $i_{j,t} = i(k_{jt}, \theta^{GJ})$. Recalling that the law of motion for those outside the financial
 39 system is given by (21), a previous non-participant enters the financial sector today
 40 at t only if

$$41 \quad k_{jt} = [\phi(k_{j,t-1}, \theta^{GJ})\eta_{jt} + (1 - \phi(k_{j,t-1}, \theta^{GJ}))\delta]i(k_{j,t-1}, \theta^{GJ}) \geq k^*(\theta^{GJ}).$$

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1 That is, the participation decision of a previously non-participating agent j at date
2 t with wealth $k_{j,t-1}$ can be rewritten as

$$\begin{aligned} 3 \quad d_{jt} &= 1, & \text{if } \eta_{jt} \geq \eta^*(k_{j,t-1}, \theta^{GJ}) \\ 4 \quad &= 0, & \text{if } \eta_{jt} < \eta^*(k_{j,t-1}, \theta^{GJ}), \end{aligned} \quad (31)$$

7 where:

$$\eta^*(k_{j,t-1}, \theta^{GJ}) \equiv \frac{1}{\phi(k_{j,t-1}, \theta^{GJ})} \left[\frac{k^*(\theta^{GJ})}{i(k_{j,t-1}, \theta^{GJ})} - (1 - \phi(k_{j,t-1}, \theta^{GJ}))\delta \right]. \quad (32)$$

13 The participation decision in (31) is stationary for a given wealth level because
14 the composite technology shock η_{jt} is drawn from the time-invariant distribution.
15 Thus once we solve the pair of functional equations in (27) and (28) to get k^* and
16 the time-invariant policy functions ϕ and i , we can form a likelihood function in
17 terms of model parameters θ^{GJ} .

18 In forming the likelihood function, the unobservable aggregate shock ζ_t gener-
19 ates cross-sectional dependence over the individuals at a given date t . Thus, we
20 first consider a *conditional* likelihood function $L_t(\theta^{GJ}, \zeta_t)$ for a given aggregate
21 shock ζ_t and then integrate the aggregate shock out to form an unconditional
22 likelihood function, as follows.

23 Given a series of serially independent aggregate shocks $(\zeta_t)_{t=1}^T$, the likelihood
24 function can be factorized into marginal likelihoods:

$$L(\theta^{GJ}, (\zeta_t)_{t=1}^T) = \prod_{t=1}^T L_t(\theta^{GJ}, \zeta_t). \quad (33)$$

29 Because the composite shock $\eta_{jt} = \epsilon_{jt} + \zeta_t$ is *i.i.d. conditional on* ζ_t , a conditional
30 likelihood function $L_t(\theta^{GJ}, \zeta_t)$ at date t is given by:

$$L_t(\theta^{GJ}, \zeta_t) = \prod_{j=1}^{n_t} [1 - \Pr(\epsilon_{jt} \leq \eta_{jt}^* - \zeta_t)]^{d_{jt}} [\Pr(\epsilon_{jt} \leq \eta_{jt}^* - \zeta_t)]^{1-d_{jt}}, \quad (34)$$

35 where $\eta_{jt}^* = \eta^*(k_{j,t-1}, \theta^{GJ})$ in (32).

36 Combining the equations (33) and (34), given the data $((k_{j,t-1}, d_{jt})_{j=1}^{n_t})_{t=1}^T$, the
37 conditional log likelihood is written as

$$\ln L(\theta^{GJ}, (\zeta_t)_{t=1}^T) \quad (35)$$

$$= \sum_{t=1}^T \sum_{j=1}^{n_t} \{d_{jt} \ln[1 - \Pr(\epsilon_{jt} \leq \eta_{jt}^* - \zeta_t)] + (1 - d_{jt}) \ln[\Pr(\epsilon_{jt} \leq \eta_{jt}^* - \zeta_t)]\}, \quad (36)$$

1 We integrate the aggregate shocks out by taking expectations in (36) with respect
2 to $\zeta = (\zeta_t)_{t=1}^T$:

$$3 \ln L(\theta^{GJ}) = E_{\zeta} \ln L(\theta^{GJ}, (\zeta_t)_{t=1}^T) \quad (37)$$

$$4 = \sum_{t=1}^T \sum_{j=1}^{n_t} E_{\zeta_t} A_{jt}(\zeta_t), \quad (38)$$

5 where

$$6 A_{jt}(\zeta_t) = d_{jt} \ln \left[\frac{1}{2} - \frac{\eta_{jt}^* - \zeta_t}{2\bar{\epsilon}} \right]$$

$$7 + (1 - d_{jt}) \ln \left[\frac{1}{2} + \frac{\eta_{jt}^* - \zeta_t}{2\bar{\epsilon}} \right], \quad \text{if } -\bar{\epsilon} \leq \eta_{jt}^* - \zeta_t \leq \bar{\epsilon}$$

$$8 = (1 - d_{jt}) * (-\infty), \quad \text{if } \eta_{jt}^* - \zeta_t \leq -\bar{\epsilon}$$

$$9 = d_{jt} * (-\infty), \quad \text{if } \eta_{jt}^* - \zeta_t \geq \bar{\epsilon}. \quad (39)$$

10 The $A_{jt}(\zeta_t)$ comes from the uniform distribution of ϵ_{jt} .¹⁹ These terms are numeri-
11 cally integrated with respect to ζ_t according to the uniform distribution over $[\underline{\zeta}, \bar{\zeta}]$
12 to get $E_{\zeta_t} A_{jt}(\zeta_t)$ in (38). We choose the parameter vector θ^{GJ} that maximizes
13 the log likelihood function in (38), satisfying the restrictions on parameter space
14 given in (22), (23), and (24).

15 In GJ, the scale parameter matters as in LEB. We choose the GJ scale of wealth
16 by matching the critical wealth level k^* with the wealth percentile \hat{k} in the data
17 such that the implied GJ participation rate in the financial sector matches the 1976
18 participation rate in the data.²⁰ That is, wealth in the Thai data is converted into
19 wealth in the GJ model using the following scale:

$$20 \text{scale}^{GJ} = \frac{k^*(\theta^{GJ})}{\hat{k}}. \quad (40)$$

21 Thus, we compute k^* before estimation to get the scale and then use the scaled
22 wealth of the data in the likelihood function. Thus, we implicitly estimate the GJ
23 scale parameter as well.

24 *4.2.2. Estimates.* We again use only the young-household sample (but for
25 all available years) for estimation because the GJ likelihood function maps the
26 *initial* wealth into the *subsequent* participation decision. Thus, we need to restrict
27 our sample for estimation to the households whose current wealth approximates
28 previous wealth. Here we again rely on the evidence on cohort age profiles of
29 wealth (Figures A.5 and A.6). The age profiles of wealth of young participants are
30 still flatter than those of the older ones, except the latest three cohorts.

31 The estimates from the MLE are reported in Table 4 with bootstrap standard
32 errors in parenthesis. The average value of log likelihood is -0.7116 . The value
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34
35

TABLE 4. Estimated GJ parameters

q	γ	β	σ	δ	$\underline{\zeta}$	$\bar{\zeta}$	$\bar{\epsilon}$
0.5021	1	0.9627	0.9946	1.0479	1.0470	1.1905	0.9954
(0.0482)	(0.0000)	(0.0061)	(0.0926)	(0.0064)	(0.0451)	(0.0514)	(0.0355)

functions v^0 and v^1 at these estimates are plotted in Figure 8, which shows the unique critical wealth level k^* of 1.0292, the crossing point of $v^0(k)$ and $v^1(k-q)$, which partitions the population into nonparticipant and participant groups. Note that the estimated fixed cost parameter q at 0.5021 is about half of this critical wealth. The estimate of γ at one (the most robust estimate) implies no variable cost. Thus, the fixed cost, not the variable cost, plays an important role in intermediation. The estimate of discount factor β at 0.9627 belongs to the range of values that are often adopted in the business cycle literature. It is interesting to note that the estimated relative risk aversion parameter is very close to one, that is, the case of log utility function as in the original GJ paper. The estimates of δ , $\underline{\zeta}$, and $\bar{\zeta}$ imply that the rates of return are 5% to safe investment and 12% to risky investment. The estimated range of idiosyncratic shock $[-0.9954, 0.9954]$ is wide enough that

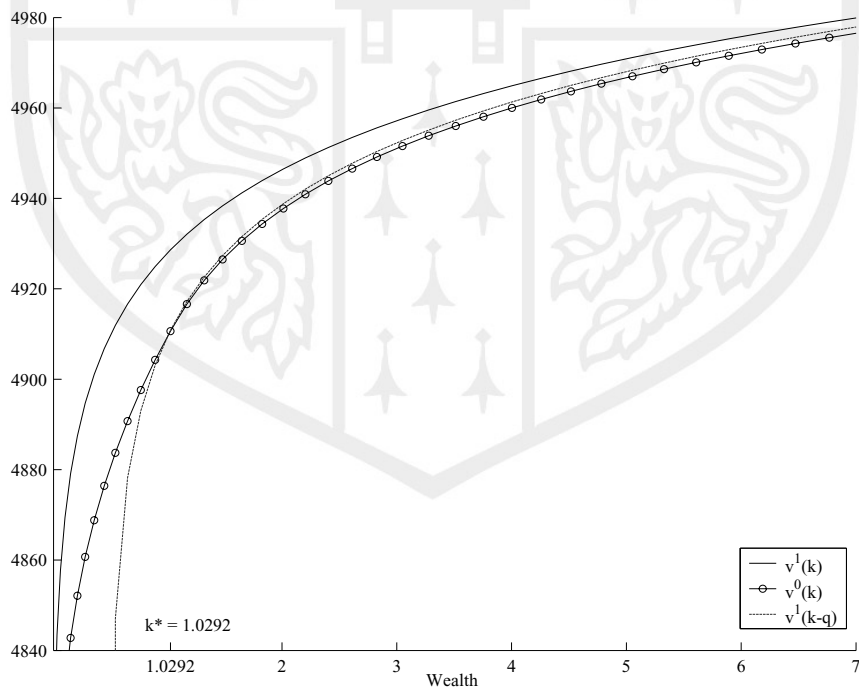


FIGURE 8. GJ value functions.

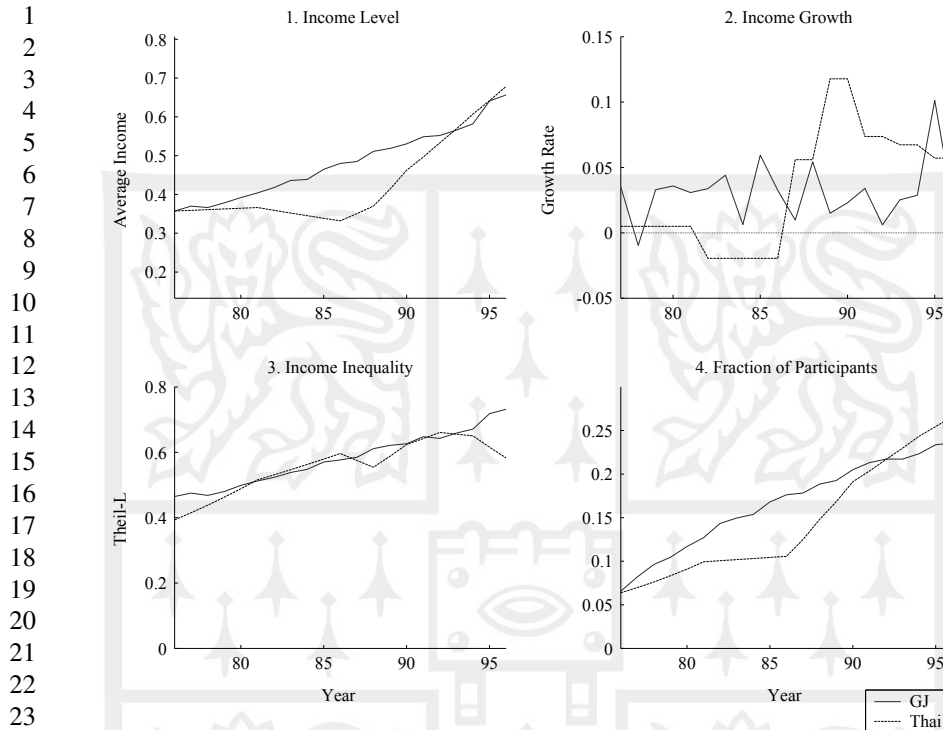


FIGURE 9. GJ aggregate dynamics.

some nonparticipants with low wealth can pay the fixed entry cost 0.5021 by a single lucky draw of idiosyncratic shock.

4.3. Evaluation

4.3.1. Aggregate dynamics. Figure 9 displays the aggregate dynamics of GJ in comparison with the Thai data. The model captures quite well the levels and overall increase in income inequality and to a lesser extent overall income growth.²¹ However, the trends are more or less linear in the model and GJ simulation captures neither the initially slow and then accelerated upturn of income growth in early 1990s nor the eventual downturn of income inequality after 1992 in Thailand. The fraction of participants in the financial sector increases both in the model and the data at similar orders of magnitudes. Again, however, the model predicts a linear trend in financial expansion, whereas the data show a clear nonlinear expansion, whereas the substantial acceleration after 1986.

4.3.2. Subgroup dynamics. Figure 10 shows the income dynamics of participant and nonparticipant groups, in comparison with those of Thailand. The growth rate of income of participants is almost always higher than that of nonparticipants

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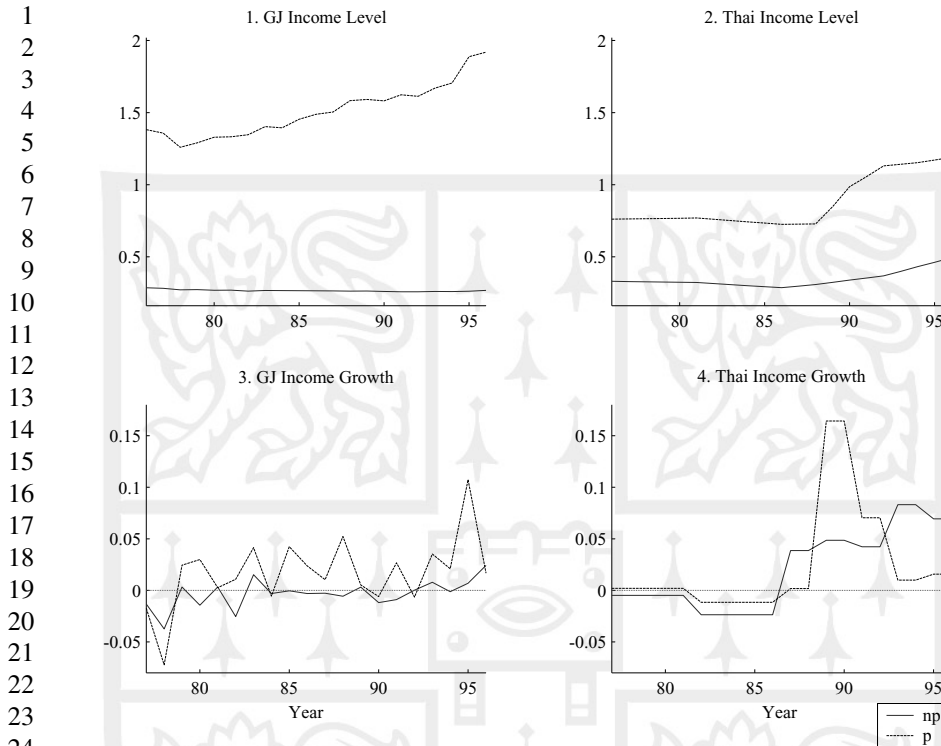


FIGURE 10. GJ subgroup growth dynamics.

in the model, and this is more or less true in the data, except for the catchup of nonparticipants after 1992. The average income grows for the participants but not for the nonparticipants in the model, while average income grows for both groups in the data. The co-movement in growth rates across participants and non-participants seems weak in the model, while it is strong in the data except for the catchup growth period after 1992. In particular, the model does not capture the growth-peak of participants during 1988–1992 and the catchup of nonparticipants after 1992.

Figure 11 compares the subgroup inequality dynamics between GJ and Thailand. Participants in the financial sector are richer than the non-participants in both the model and the data, a source of across-group inequality. The income ratio of the participant group to the non-participant group widens over time from 5 to 7 in the model, while it increases only moderately from 2.3 to 2.4 (peaking at 3.1 in 1992) in the data. The increase in inequality from the divergence in income levels across the two groups is a mirror image of growth features in GJ. The benefits of better investment are available only to the participants in the financial sector and they have a higher income growth than the nonparticipants. Incomes

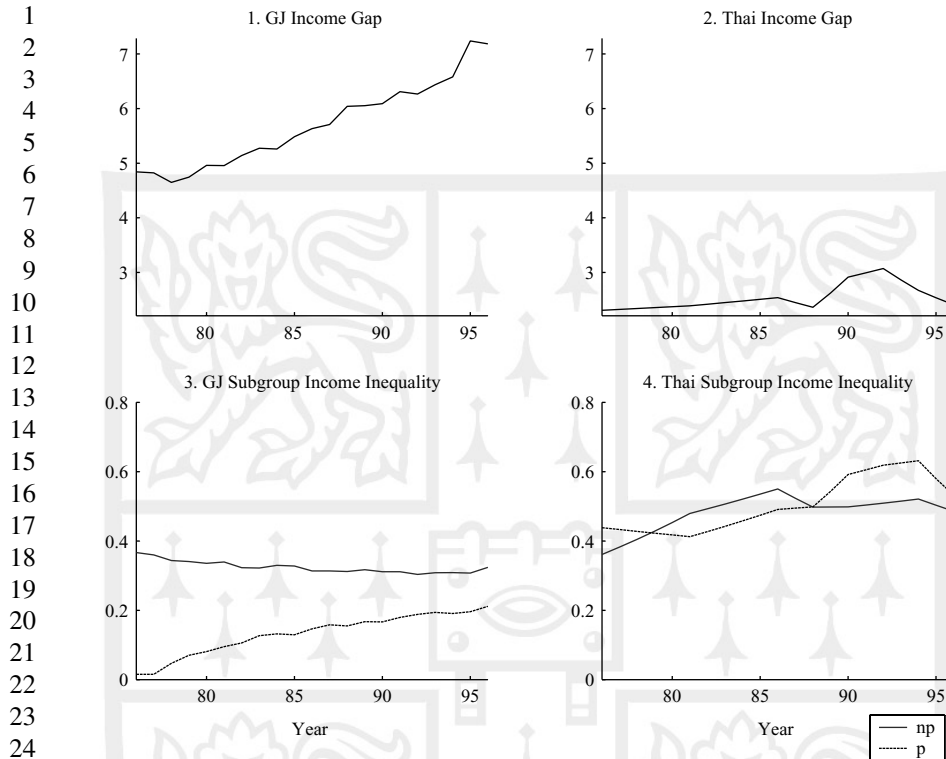


FIGURE 11. GJ subgroup inequality dynamics.

of nonparticipants also grow, but the rich households among them keep exiting to the participant group. These two effects within the nonparticipant group appear to offset one another in the model, keeping levels flat and average income growth among nonparticipants close to zero (see Figures 10.1 and 10.3).

GJ predicts that the poor group (nonparticipants) has higher inequality than the rich group (participants). However, inequality increases only among the participants, and it is stable (slightly decreasing) among the nonparticipants. These subgroup inequality features are related also to the entry-exit dynamics: the upper tail of the income distribution among nonparticipants is trimmed by exit, and the new entrants to the financial sector, poorer than the incumbents in the financial sector, are continually added to the lower tail of the income distribution of the participants. In contrast, in the data, there is no clear inequality ordering between the two groups and inequality increases for both of them, following a more or less common trend. This suggests that GJ seems to miss some driving forces of increase in inequality, common to both participants and nonparticipants, for example, educational expansion.²²

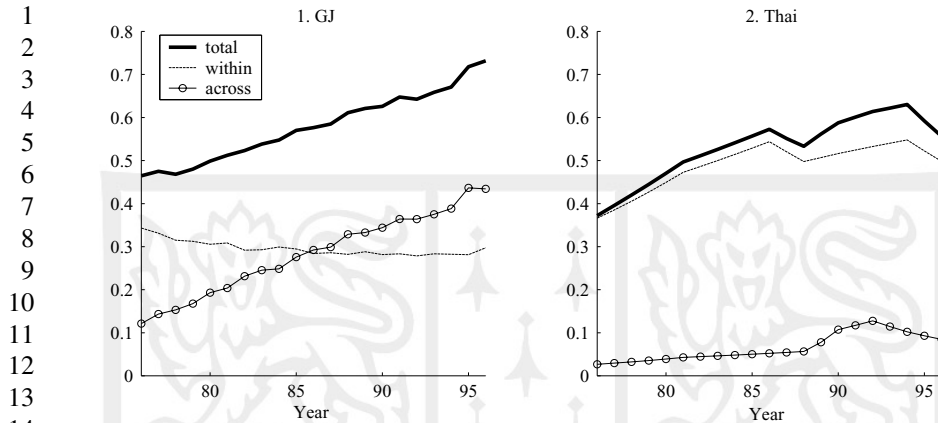


FIGURE 12. Within vs. across inequality decomposition.

The level of inequality is close to the data for the nonparticipant group, but it is much lower than the data for participant group. The diversification of idiosyncratic shocks in the financial sector of GJ seems excessive relative to the actual income variation among the participants in the data.

4.3.3. Decomposition. We apply the same decomposition methods in Section 2, with respect to financial sector participation. Total inequality is decomposed into within-group inequality and across-group inequality in Figure 12, comparing GJ to Thailand. In terms of both trends and patterns of movement over time, the driving force of inequality dynamics in GJ is across-group inequality, whereas it is within-group inequality in Thailand.

The two-decade growth rates of mean income and income inequality are decomposed in Tables 5 and 6, respectively. The model predicts a growth rate of mean income at 0.838, quite close to that of Thailand at 0.899. The composition effect of increasing participation in the financial sector on growth in GJ is substantial (at the rate of 0.654), as in the data (at the rate of 0.319). This composition effect is the main source of growth in GJ. Still, contribution of subgroup growth is larger than that of compositional growth in Thailand.

The model predicts an increase in income inequality over two decades, as in the data, but, with the predicted continual increase in inequality, the overall increase

TABLE 5. Decomposition of aggregate income growth in GJ

	Subgroup	Composition	Total
Thailand	0.580	0.319	0.899
GJ	0.184	0.654	0.838

TABLE 6. Decomposition of aggregate inequality change in GJ

	Within-Group		Across-Group		Total
	Subgroup	Composition	Income Gap	Composition	
Thailand	0.304	0.032	0.015	0.133	0.483
GJ	-0.014	-0.085	0.295	0.338	0.575

is higher in the model at 0.575 than in the data at 0.483. The composition effect, that is, the population shift from the nonparticipant group to the participant group, on across-group inequality change is substantial in the model (at the rate of 0.338) as in the data (at the rate of 0.133). As just noticed in Table 5, this population shift is also the source of income growth, so that the financial sector expansion is a significant link between growth and inequality dynamics both in the model and in the data. However, the effects in the model are exaggerated for both growth and inequality change; the orders of magnitudes in the model are larger than in the data. The divergence in income levels across the non-participant group and the participant group contributes to an increase in across-group inequality in the model at 0.295. The divergence is also observed in the data, but again with a much smaller order of magnitude at 0.015.

The composition effect contributes to a decrease in within-group inequality at low rate of -0.085 in the model because of population shifts from the high-inequality group (nonparticipants) to the low-inequality group (participants). The inequality ordering over the two groups is the opposite in the data, and so population shift contributes to an increase in within-group inequality. However, these effects are small in both model (-0.085) and data (0.032). The principal difference in inequality dynamics between model and data lies in the effect of changes in subgroup inequality on total inequality change. This effect is very small in the model but the most important source of inequality change in the data.

In sum, the effects of population shifts and income gaps across key groups in the model are overemphasized and subgroup effects are underemphasized relative to the data for both growth and inequality change. However, endogenizing financial participation in GJ solves the previous puzzles in LEB (where the participation was exogenously imposed), namely, lower income of the participants than the nonparticipants for entrepreneurs, convergence in income levels between the two groups, and a decrease in inequality among participants.

4.3.4. End-of-sample-period income distribution. Figure 13 compares the cumulative distribution function of income at the end of sample period, 1996, of the GJ model to that of the Thai data. The lower tail of the distribution is shifted to the left in the model as compared to the data. That is, the model predicts a high fraction of poor people relative to the data. The middle range of the distribution is flat in the model, that is, the model predicts a sparse middle class relative to

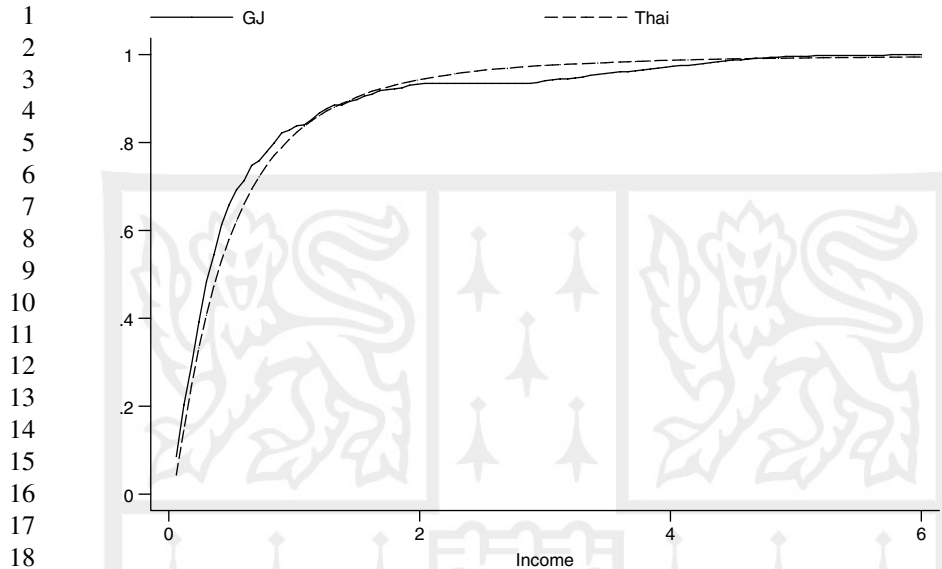


FIGURE 13. CDF of 1996 income distribution.

the data. This is due to the common fixed entry cost to the financial sector, that is, a common fixed sum of wealth is subtracted for new entrants into the financial sector. The distribution reaches unity at lower level of income in the model than in the data. That is, the model again does not capture the extremely rich people in the data.

We apply the Kolmogorov-Smirnov goodness-of-fit test to the GJ end-of-sample-period income distribution. The KS statistic is 0.58 (corresponding p-value is 0.89) and the null hypothesis of similarity of income distributions between the GJ model and the Thai data is accepted. Thus, despite the observed discrepancies above, overall shape of income distribution is quite well captured by the GJ model.

4.4. Sensitivity Analysis

All GJ parameters are estimated. To perform a sensitivity analysis, we vary the parameter values within one-standard-error bands around the point estimates. We fix γ at one because it is always pushed to this boundary value in estimation. Here bear in mind that for each variation of parameter values, the series of best-fitting realizations of aggregate shocks differs from the benchmark ones.

All features of GJ dynamics (income growth, inequality change, and financial expansion) are robust to the perturbation of preference parameter σ , fixed entry cost q , and idiosyncratic shock parameter $\bar{\epsilon}$ within their one-standard-error bands. An increase in σ makes the agents more risk averse and reduces the share of risky investment (that has a higher expected return) of the nonparticipants. This increases the value of risk-sharing as well as the income gap between participants

1 and nonparticipants. Thus average income growth becomes smaller and inequality
 2 increase becomes larger. The effects of varying q are not certain *a priori*. As q
 3 increases, k^* also increases because the ratio of the two remains the same. This
 4 makes the economy wealthier, because of an increase in GJ scale in equation (40).
 5 An increase in q *per se* hinders non-participants from entering the financial sector,
 6 but the associated increase in wealth helps participation. Also an increase in q
 7 implies more lump sum payment of resources that are not used for investment.
 8 This may lower overall growth but the income gap between participants and
 9 nonparticipants may become smaller. Within the one-standard-error increase in q ,
 10 the income growth rate is lower, inequality increases less, and participation rate is
 11 higher.

12 An increase in $\bar{\epsilon}$ implies an increase in the variance of idiosyncratic shock
 13 and makes the value of risk-sharing larger. In turn, participation in the financial
 14 sector is more attractive, but nonparticipants' income growth becomes lower. This
 15 results in lower average income growth and a higher rate of increase in inequality.
 16 However, the orders of magnitude of the changes in aggregate dynamics from
 17 perturbing parameters σ , q and $\bar{\epsilon}$ are small. Figure A.9 shows that by increasing
 18 $\bar{\epsilon}$ from 0.9954 to 1.0309, the annual average income growth rate decreases from
 19 3.09% to 3.06%, and the rate of change in inequality increases from 2.30% to
 20 2.72% per year. The end-of-sample-period fraction of participants increases from
 21 23% to 27%.

22 Income growth and financial expansion turn out to be sensitive to aggregate
 23 shock parameters ζ , $\bar{\zeta}$ (which determine the rate of return to the risky investment),
 24 safe return δ , and discount factor β (which determine the utility return to saving),
 25 but inequality dynamics remain relatively robust. An increase in ζ increases the
 26 expected return to risky investment and reduces the variance of aggregate shock.
 27 This makes the risky investment more attractive, and aggregate income growth
 28 and the shift to financial sector become faster. But this benefits participants more
 29 than nonparticipants, and income gap between them diverges faster. Figure A.10
 30 displays that an increase in ζ from 1.0470 to 1.0921 (the most sensitive case of
 31 all experiments) increases income growth rate from 3.09% to 5.99%, and makes
 32 income inequality grow at the rate of 4.69% per year. The end-of-sample-period
 33 fraction of participants increases to 36%.

34 An increase in $\bar{\zeta}$ increases the expected return to risky investment and its
 35 variance as well. Thus whether it makes the risky investment more attractive for
 36 the nonparticipants is uncertain, but it increases the value of advanced information
 37 on aggregate shock and hence the benefits from participation. Within the one-
 38 standard-error band, an increase in $\bar{\zeta}$ induces more income growth, faster financial
 39 expansion, and faster increase in inequality. An increase in δ benefits both partic-
 40 ipants and nonparticipants. Income growth is higher but the inequality dynamics
 41 remain about the same. The financial expansion is faster because of higher wealth
 42 accumulation on the part of nonparticipants. An increase in β makes the all agents
 43 more patient, and total investment increases. Its effects are similar to the increase
 44 in δ .

1 In summary, income growth and financial expansion are sensitive to parameters
2 that determine the rates of return to investment, in particular the risky one, and
3 less sensitive to the parameters of risk aversion, entry cost, and the idiosyncratic
4 shock. The Ak nature of GJ technology seems to lie behind this result. Furthermore,
5 the benefits of intermediation in the GJ model are driven more by the value of
6 advanced information on aggregate shock (determined by ζ , $\bar{\zeta}$, and δ) than by the
7 risk-sharing on the idiosyncratic shocks (determined by $\bar{\epsilon}$). Inequality dynamics
8 remain robust to most perturbations.²³

10 5. CONCLUSION

11 We evaluated two well-known macro models of growth and inequality which are
12 built on explicit micro underpinnings and impediments to trade, that is, wealth-
13 constrained self-selection. A two-step evaluation scheme was adopted. In the
14 first step, we estimated most key parameters by fitting the assumed individual
15 selection decisions of households without using the implied aggregate dynamic
16 data. In the second step, we simulated the aggregate dynamics of growth and
17 inequality together with subgroup dynamics of the models at those micro-fitted
18 parameters and compared the predictions to the actual data. Thus, we use theories
19 both for estimation and simulation. Explicit use of structural models and the
20 framework of computational experiments, described by Kydland and Prescott
21 (1996), helped us to organize our theoretical perspectives as well as the empirical
22 data. However, explicit use of estimation also helped us to make consistent use
23 of postulated economic environments and data. The importance of the latter has
24 been emphasized by Hansen and Heckman (1996).

25 Not all available data were used in estimating parameters. Only the cross-
26 sectional micro data on self-selection and wealth were used with likelihood meth-
27 ods to estimate key parameters. The aggregate dynamics and income distribution
28 data were saved for testing. This separated use of data, estimation versus test-
29 ing, helped us to avoid the potential danger of *ad hoc* overfitting, as addressed
30 by Granger (1999). Our two-step micro-macro empirical strategy contributes to
31 the synthesis between micro evidence and macroeconomic theory, envisioned by
32 Browning, Hansen, and Heckman (1999).

33 Experimenting with two different models of growth and inequality and compar-
34 ing them was helpful in identifying the salient patterns of the data and in
35 documenting anomalies of the models. The parameter values chosen from cross-
36 sectional micro estimation were not picked to generate nice aggregate dynamics.
37 Surprisingly, however, the simulated aggregate dynamics of growth and inequal-
38 ity are close to the actual data for both models. In particular, LEB captures the
39 aggregate movements of growth and inequality through endogenous factor price
40 movements without aggregate shocks. GJ also does well with the long-run trend
41 of growth with increasing inequality but not with the nonlinear patterns of income
42 growth and inequality change.

43 Each model can predict compositional changes in the population across key
44 selection groups as in the data. The effects of compositional changes on both

1 income growth and income inequality change are substantial in each model and
2 also in the data. This confirms Kuznets's (1955) hypothesis on the existence of a
3 macro relationship between growth and inequality, but here *via micro channels* of
4 wealth-constrained self-selection.

5 However, we also observed several anomalies. First, income gaps across key
6 subgroups are too high in the models relative to the data. Second, neither model
7 can predict the co-movement patterns across subgroups observed in the data.
8 Third, neither model can replicate the movements of aggregate income growth
9 and income inequality in relation to the growth patterns of entrepreneurs in the
10 financial sector (the smallest but richest group). Fourth, income variation at the tails
11 of the income distribution, in particular at the lower tail, are not well captured. The
12 reasons for the anomalies are different across the two models, but the fundamental
13 sources seem to be lack of appropriate aggregate shocks and heterogeneity. Still,
14 from the comparative evaluation of two models, we learned that the simple addition
15 of aggregate shocks and the introduction of more kinds of heterogeneity improve
16 neither aggregate dynamics nor cross-sectional income distribution patterns. What
17 matters is exactly *how* aggregate shocks and heterogeneity are incorporated, not the
18 adding aggregate shocks or more kinds of heterogeneity itself. The GJ model, with
19 aggregate shocks incorporated, captured the movements of aggregate income level
20 and inequality worse than the LEB model that has no aggregate shocks. However,
21 though having less kinds of heterogeneity, the GJ model with its endogenously
22 structured costly access to the financial sector could remedy many of the anomalies
23 of LEB.

24 Low within-group inequality among participants in financial sector suggests that
25 insurance for idiosyncratic shocks in the model is overdone. Lack of co-movement
26 across subgroup growth rates suggests that the informational advantage of financial
27 sector in processing aggregate risk is too perfect. Ironically, high entrepreneurial
28 income inequality among financial participants in LEB pushes one in the same
29 direction. Thus, less perfect and less uniform financial markets for those with
30 access are another promising feature to be incorporated.

31 We also learned that model specification and model evaluation are intimately
32 related to each other. There is a thin edge between calibration and estimation that
33 must be faced even if it appears in only one parameter, in our exercise in LEB.
34 The support of idiosyncratic shock, the random setup cost, is bounded and fixed,
35 as the shock enters the model in an additive way. Thus the choice of scale that
36 converts wealth in the data into wealth in model units becomes important in both
37 estimation and simulation. In fact, for some range of scales, there exists a trade-off
38 between likelihood values from cross-sectional estimation and goodness-of-fit in
39 simulated dynamics. However, once a scale parameter was chosen, most of key
40 parameters of preferences and technology could be identified from explicit estima-
41 tion with cross-sectional data alone. Thus, we were able to implement our two-step
42 strategy.

43 We hope that our work here will enhance the synthesis between micro evidence
44 and macroeconomic theory and allow an improved understanding of the rela-
tionship between growth and inequality. We also hope that our proposed model

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1 evaluation strategy can help to guide future research to advance the mutual pene-
 2 tration of quantitative economic theory and statistical observation.

3
4
5 NOTES

6 1. For a critical review of the diverse cross-country analysis results, see Jeong (2000) and Banerjee
 7 and Duflo (2000).

8 2. In fact, Jeong and Townsend (2007) choose the parameters of one of the benchmark models of
 9 this paper [a modified Lloyd-Ellis and Bernhardt (2000) model] matching the *aggregate dynamics* of
 10 output growth and factor shares (not the household choices) to explain the *components* of total factor
 11 productivity (TFP).

12 3. The regional average Gini coefficients are from Deininger and Squire (1996).

13 4. Banerjee and Newman (1993) and Aghion and Bolton (1997) also provide equilibrium theories
 14 of growth and inequality in relation to occupational choice and financial market imperfection, but in
 15 aggregate contexts. Jeong and Kim (2006) study complementarity between sector-specific experience
 16 and labor as another channel of earnings growth and inequality during transition to modern economic
 17 growth. They bring the model to the same Thai data applying a similar empirical strategy of simulation
 18 of aggregate dynamics of growth and inequality at the micro-fit parameters estimated from a cross-
 19 sectional earnings equation.

20 5. Specific form of z function is derived in Appendix A.2.

21 6. This limited use of data helps us to avoid the following endogeneity issue. Suppose we observe
 22 a wealthy household whose occupational choice is an entrepreneur. Then, it can be either the case that
 23 the household is wealthy because of its previous occupational choice as entrepreneur, or the case that
 24 it chose to be an entrepreneur because of its high initial wealth. Using the entire sample, we cannot
 25 distinguish between the two cases.

26 7. To check the robustness of the estimates, we varied the sample of young households by changing
 27 the cutoff age to 25 and also to 35 and got similar estimates. As the average age of Thai household
 28 heads is 45, this range of variation in identifying young households seems reasonable.

29 8. The bootstrap was run with 10,000 random resamplings with replacement. The standard errors
 30 are reported in scale of 10^{-12} .

31 9. A referee suggests that the relative precision levels across the estimates appear to be counter-
 32 intuitive, observing that the curvature parameters ξ , ρ and σ are much more precisely estimated than
 33 the slope parameters α and β . Although the referee mistakenly categorize between curvature and slope
 34 parameters (in fact, β , ρ and σ are curvature parameters and α and ξ are slope parameters), this is
 35 an interesting question worth to discuss, leading to a better understanding of the nature of the LEB
 36 estimation. Related, the referee also seeks why we have $\alpha \simeq 1$ and $\sigma = 0$. Note that the likelihood is
 37 written on occupational choices, not directly on production function. Thus, it is the three curvature
 38 parameters $x^*(w)$, $b^*(w)$ and $\tilde{b}(w)$ of the critical setup cost function $z(b, w)$ (or equivalently the
 39 curvature parameters of profit function, see Appendix A.2) in relation to the occupational choice
 40 data, not those of production function, which determine the precision as well as the values of the
 41 estimates. The parameters ξ and ρ are precisely estimated because $\tilde{b}(w) = \frac{(\xi-w)^2}{2\rho} - w$ is precisely
 42 estimated. α is estimated close to one σ is (tightly) estimated at zero because the gap $x^*(w) -$
 43 $\tilde{b}(w) = \frac{\rho(\alpha-1)}{2(\rho\beta-\sigma^2)} + \sigma \frac{\rho(\xi-w)}{2(\rho\beta-\sigma^2)}$ is estimated very small and does not depend on wage w , implying
 44 $\alpha \simeq 1$ and $\sigma = 0$. These technology parameters estimates (in particular $\sigma = 0$) obtained fitting the micro
 occupational choices put restrictions on aggregate dynamics.

10. This can happen as a result of the myopic nature of the LEB preferences.

11. We normalize the Thai income unit by matching the 1976 mean income levels between the
 model and the data for the sake of convenient comparison. This normalization does not affect the
 inequality levels in the data.

12. The decomposition of ΔAI involves a log approximation. See Mookherjee and Shorrocks
 (1982).

1 13. The discrepancy between the sum of component changes and the total change is a result of the
2 log approximation in (12).

3 14. We generate the empirical distribution functions with sample size of 100 for both the LEB
4 model and the Thai data. The p-value is from Smirnov (1948).

5 15. In fact, the dynamics are robust to the variation of α , β , and σ over the *entire* ranges, not
6 just within 10-percent-deviation ranges, of the parameter space that satisfy the restrictions of the LEB
7 model, which are $[1, 1.3]$ for α , $[0.01, \infty)$ for β , and $[0, 0.013]$ for σ .

8 16. See Appendix A.2.

9 17. In their original model, GJ consider a log utility function, a special case of the CRRA preferences
10 with $\sigma \rightarrow 1$.

11 18. See Townsend and Ueda (2006) for full discussion.

12 19. The latter two lines in (39) define zero-probability events of corner solutions.

13 20. The \hat{k} , the top 6.4 percentile wealth in 1976, is 204,824 baht in the data.

14 21. Again, we normalize the Thai income unit by matching the 1976 mean income levels between
15 the model and the data.

16 22. See Jeong (2000) for the important role of educational expansion on increase in inequality in
17 Thailand.

18 23. In contrast, in LEB, inequality dynamics were much more sensitive than income growth and
19 occupation choice dynamics.

20 24. In the 1976 SES, financial income was not recorded separately and thus cannot be added to the
21 total income for this year.

22 25. There are other asset items recorded in the SES, depending on years. We choose the items that
23 are commonly collected across all sampling years.

24 26. This single proxy variable accounts for 26 to 36% of the total variation of the ownership of
25 sixteen assets. The scoring coefficients of the first principal component are available upon request.

26 27. To calculate the representative interest rate, we use the time-series of average of the lending
27 rates of commercial banks, finance companies, and interbank loans between 1978 and 1996. (Data
28 source: Economic Research Department at the Bank of Thailand.)

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APPENDIX

A.1. DATA DESCRIPTION

32 We use the Thai Socio-Economic Survey (SES), a nationally representative micro survey
 33 conducted by the National Statistical Office in Thailand. Over the recent two decades,
 34 between 1976 and 1996, eight rounds of repeated cross-sections were collected: 1976, 1981,
 35 1986, 1988, 1990, 1992, 1994, and 1996, using a clustered random sampling, stratified by
 36 geographic regions over the entire country. The sampling unit is household and the sample
 37 size varies from 10,897 to 25,208, becoming larger in later years. Economically active
 38 households in the SES data were selected for our analysis.

39 The income is measured in real annual terms in 1990 baht value, which includes
 40 earned income (profit income for the self-employed and wage income for the work-
 41 ers) and financial income (land rents, interest and dividend income from financial
 42 investment).²⁴

43 For a binary occupation category, we call entrepreneurs by the nonfarm business house-
 44 holds and the rest are categorized into nonentrepreneurs. For a financial participation
 category, we identify the participants with the households who actually made financial

1 transactions with any of the formal financial intermediaries—commercial banks, a gov-
 2 ernment savings banks, the Bank of Agriculture & Agricultural Cooperatives (BAAC),
 3 a government housing bank, financial companies, or credit financiers, and the rest are
 4 nonparticipants.

5 The SES does not directly record total wealth data, but it does record various wealth
 6 items. Using the information on these wealth items, we construct a proxy for household
 7 wealth. We first use the information on ownership of sixteen household assets: private
 8 water supply, gasoline-cooking equipment, access to electricity, phone, sofa, bed, stove,
 9 refrigerator, electric iron, electric pot, radio, TV, motorcycle, car, sewing machine, and
 10 motor boat.²⁵ Applying principal-component analysis to these variables, we pick the first-
 11 principal component, which best summarizes the variations of the ownership of the sixteen
 12 assets by a single variable, as a proxy for the latent wealth underlying them.²⁶ This asset
 13 index is not in monetary units. To convert it into monetary unit, we use the rental value
 14 of owned house as the representative rental price and multiply the above asset index by
 15 the rental price. This gives an approximate estimate of *flow value* of the above sixteen
 16 assets. We add other rental incomes to this to get the total flow value of wealth. We then
 17 divide this flow value of wealth by the interest rate to get an estimate of *stock value* of
 18 wealth.²⁷

19 A.2. LEB IDENTIFICATION

20 For the quadratic form of technology,

$$21 \quad f(k, l) = \alpha k - \frac{\beta}{2} k^2 + \xi l - \frac{\rho}{2} l^2 + \sigma lk,$$

22 labor demand l is linear in capital demand k

$$23 \quad l = \frac{\xi - w}{\rho} + \frac{\sigma}{\rho} k, \quad (\text{A.1})$$

24 and profit function can be expressed as a second-degree polynomial of capital demand k :

$$25 \quad \pi(b, x, w) = C_0(w) + C_1(w)k + C_2k^2 - x, \quad (\text{A.2})$$

26 where

$$27 \quad C_0(w) = \frac{(\xi - w)^2}{2\rho}, \quad (\text{A.3})$$

$$28 \quad C_1(w) = \alpha - 1 + \frac{\sigma(\xi - w)}{\rho}, \quad (\text{A.4})$$

$$29 \quad C_2 = \frac{1}{2} \left(\frac{\sigma^2}{\rho} - \beta \right). \quad (\text{A.5})$$

30 Capital demand k depends on wealth b as well as technology parameters $(\alpha, \beta, \xi, \rho, \sigma)$
 31 and market wage w , if the entrepreneurs are constrained. Unconstrained capital demand k^* ,
 32 independent from wealth, is given by

$$33 \quad k^* = \frac{C_1(w)}{-2C_2}.$$

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1 Note that the key determinant in occupational choice is the critical setup cost function
 2 $z(b, w)$, which is derived by equating the above profit function in (A.2) with wage w . Let
 3 $b^*(w)$ be the critical level of wealth above which the wealth constraint does not bind in
 4 occupational choice, $x^*(w)$ be the associated level of critical setup cost, and $\tilde{b}(w)$ be the
 5 wealth level below which the wealth constraint binds exactly at the level of setup cost
 6 (hence the capital demand hits the lower bound zero). These three objects $b^*(w)$, $x^*(w)$,
 7 and $\tilde{b}(w)$, conditional on wage w , fully characterize the occupational choice in the LEB
 8 model and the z function is given as.

$$\begin{aligned} z(b, w) &= x^*(w), & \text{if } b \geq b^*(w) & & \text{(A.6)} \\ &= b + \frac{C_1(w) + 1 - \sqrt{(C_1(w) + 1)^2 - 4C_2(C_0(w) - b - w)}}{2C_2}, & & & \\ & & \text{if } \tilde{b}(w) \leq b < b^*(w) & & \\ &= b, & \text{if } b < \tilde{b}(w), & & \end{aligned}$$

16 where

$$\tilde{b}(w) = C_0(w) - w, \quad \text{(A.7)}$$

$$x^*(w) = \tilde{b}(w) - \frac{C_1(w)^2}{4C_2}, \quad \text{(A.8)}$$

$$b^*(w) = x^*(w) - \frac{C_1(w)}{2C_2}. \quad \text{(A.9)}$$

24 That is, the three coefficients $C_0(w)$, $C_1(w)$, and C_2 , of profit function determine not only
 25 the income of entrepreneurs but also the occupational map. Thus, the LEB log likelihood
 26 function can be reduced into the following form:

$$\log L(\alpha, \beta, \xi, \rho, \sigma, m; w) = \log L(C_0, C_1, C_2, m; w)$$

27 and only three out of five production parameters can be identified if a *single* wage is used.

31 Unlike the models with a Cobb-Douglas production function, factor income shares are
 32 not stationary in LEB and they cannot be used in pinning down the remaining technology
 33 parameters. However, by *adding variation in wage*, we can uncover the full five production
 34 parameters as follows. Suppose we use wage variation over time, say between two initial
 35 years, 1976 and 1981. Given the wage in 1976, w^{76} , the critical setup cost function z and
 36 the log likelihood function are characterized by the three coefficients $C_0(w^{76})$, $C_1(w^{76})$,
 37 and C_2 , and similarly the $C_0(w^{81})$, $C_1(w^{81})$, and C_2 , at the wage in 1981, w^{81} . Note that
 38 the coefficient C_2 does not depend on wage, and should be the same over time. This plays
 39 a role of an identifying restriction. We form the log likelihood function over the two years

$$\log L(C_0^{76}, C_1^{76}, C_2, m; w^{76}) + \log L(C_0^{81}, C_1^{81}, C_2, m; w^{81}), \quad \text{(A.10)}$$

42 where $C_0^{76} = C_0(w^{76})$, $C_1^{76} = C_1(w^{76})$, $C_0^{81} = C_0(w^{81})$, and $C_1^{81} = C_1(w^{81})$. By allowing
 43 exogenous growth in the subsistence income γ , the reservation wage level will also exoge-
 44 nously vary over time. Thus we can avoid the endogeneity problem in our estimation using

1 two different wage rates at initial years, during which the slow wage growth in Thailand is
2 considered as the exogenous reservation wage growth.

3 Now we estimate C_0^{76} , C_1^{76} , C_0^{81} , C_1^{81} , and C_2 by maximizing the log likelihood function
4 in (A.10). Then, the five production parameters (α , β , ξ , ρ , σ) can be identified as follows.
5 First, from dividing C_0^{76} by C_0^{81} , we find ξ :

$$6 \quad \xi = \frac{w^{81} \sqrt{C_0^{76}} - w^{76} \sqrt{C_0^{81}}}{\sqrt{C_0^{76}} - \sqrt{C_0^{81}}}. \quad (\text{A.11})$$

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9 Then, substituting this ξ either into C_0^{76} or into C_0^{81} , we find ρ :

$$10 \quad \rho = \frac{1}{2} \left(\frac{w^{81} - w^{76}}{\sqrt{C_0^{76}} - \sqrt{C_0^{81}}} \right)^2. \quad (\text{A.12})$$

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12
13 Using this ρ and subtracting C_1^{76} from C_1^{81} , we get σ :

$$14 \quad \sigma = \frac{1}{2} \frac{(w^{81} - w^{76})(C_1^{76} - C_1^{81})}{\left(\sqrt{C_0^{76}} - \sqrt{C_0^{81}}\right)^2}. \quad (\text{A.13})$$

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17 Substituting these ξ , ρ , and σ either into C_1^{76} or into C_1^{81} , α can be found:

$$18 \quad \alpha = 1 + \frac{C_1^{81} \sqrt{C_0^{76}} - C_1^{76} \sqrt{C_0^{81}}}{\sqrt{C_0^{76}} - \sqrt{C_0^{81}}}. \quad (\text{A.14})$$

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21 Finally, substituting ρ , and σ into C_2 , we get β :

$$22 \quad \beta = \frac{1}{2} \left(\frac{C_1^{76} - C_1^{81}}{\sqrt{C_0^{76}} - \sqrt{C_0^{81}}} \right)^2 - 2C_2. \quad (\text{A.15})$$

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24
25 The support of the setup cost x is specified as unit interval, and the critical values \tilde{b} and
26 x^* in the z function should satisfy the following relations:

$$27 \quad 0 \leq \tilde{b}(w^t) \leq 1,$$

$$28 \quad 0 \leq x^*(w^t) \leq 1,$$

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31 which implies that C_0^t , C_1^t , and C_2 should satisfy

$$32 \quad C_0^t - w^t \geq 0, \quad (\text{A.16})$$

$$33 \quad C_0^t - w^t - \frac{C_1^{t2}}{4C_2} \leq 1. \quad (\text{A.17})$$

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1 Furthermore, since z is increasing and concave in b , the following restrictions should be
 2 met:

$$3 \quad \tilde{b}(w^t) \leq x^*(w^t),$$

$$4 \quad x^*(w^t) \leq b^*(w^t),$$

5
 6 which again implies that

$$7 \quad C_2 \leq 0, \quad (\text{A.18})$$

$$8 \quad C'_1 \geq 0. \quad (\text{A.19})$$

9
 10 The inequality constraints from (A.16) to (A.19) restrict the LEB parameter space and are
 11 imposed in estimation.

12 A.3. LEB SIMULATION ALGORITHM

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 14 The LEB model is simulated using the algorithm of Gine and Townsend (2004). At every
 15 date there is a distribution of beginning-of-period wealth, presumed to lie on some a
 16 priori grid. Guessing a wage, along with the parameters of technology, the regions of
 17 the occupation partition are pinned down. The distribution of talent then determines the
 18 fractions of the population choosing to be workers, subsisters, or entrepreneurs at each
 19 level of wealth. Adding up over all wealth levels, these population fractions should sum
 20 to one, and otherwise the labor market does not clear. This procedure is repeated to find
 21 an equilibrium wage in a bisection algorithm. Thus, end-of-period wealth is determined.
 22 A fraction ϖ of this wealth is saved, and this determines next period's distribution of
 23 beginning-of-period wealth. The distribution of setup cost for entrepreneurs adds additional
 24 diversity. The lower end point of the wealth distribution is the wealth of the household in
 25 the previous period who had least beginning-of-period wealth and the lowest talent (highest
 26 setup cost), and the upper end point is associated with the household in the previous period
 27 who had the highest beginning-of-period wealth and the highest talent (lowest setup cost).
 28 The initial condition of the model is the estimated initial distribution of wealth. Here we take
 29 the 1976 SES wealth distribution, scaled by the chosen wealth scale used in the estimation,
 30 as the initial wealth distribution for simulation. One period in the simulation corresponds
 31 to one year in the data.

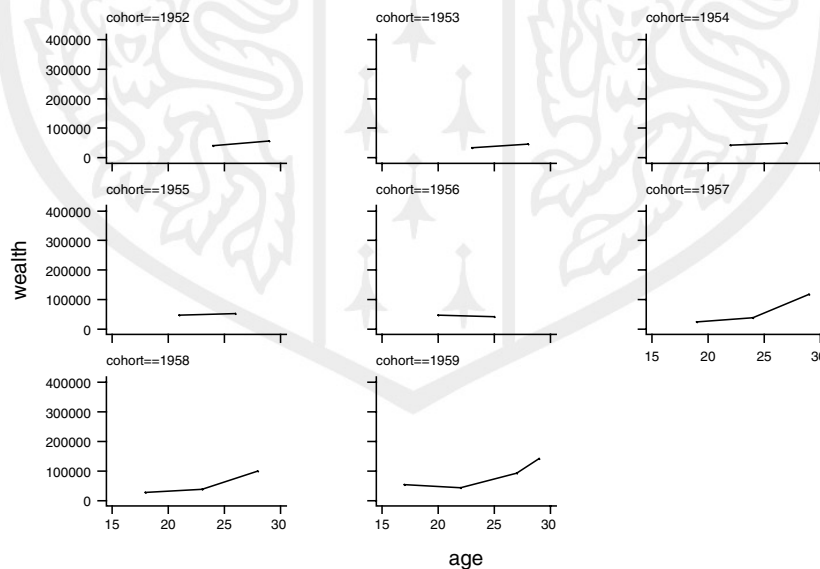
32
 33 In the data, there are households who indeed have access to financial sector. Because
 34 the original LEB model does not distinguish between the participants and non-participants
 35 in the financial sector, it is modified to include an exogenously embedded intermediated
 36 sector. Those in the intermediated sector can borrow and lend their wealth at an equilibrium
 37 interest rate, determined in a bisection algorithm. In this sector, the occupational map of
 38 Figure 1 is completely flat. That is, wealth does not determine occupational choice or scale
 39 of enterprise. There is only a common critical value for setup cost. This sector is otherwise
 40 integrated with the rest of the economy via a common labor market and hence a common
 41 market wage. Thus, the wage and interest rate are determined simultaneously. At each
 42 period, the number of households in the intermediated sector is specified exogenously, and
 43 made to increase at the observed rate of increase in participation as in the SES data, from
 44 6% in 1976 to 26% in 1996.

1 A.4. GJ SIMULATION ALGORITHM

2 The GJ model is simulated using the algorithm of Townsend and Ueda (2006). The burden
 3 here is finding the value functions v^0 and v^1 described earlier, which are not bounded, and
 4 the support of which is evolving over time. Still, the value function v^1 has a closed form
 5 solution up to the risk aversion parameter σ , as does a value function for a fictitious sector,
 6 those never allowed to enter the financial system. The value function v^0 can be trapped
 7 between these two. The non-convex aspect of the problem, the one associated with the fixed
 8 entry cost q , disappears in the limit, as the horizon is driven to infinity. The value functions
 9 converge after iteration. The space of value functions is reasonably well approximated by
 10 Chebyshev polynomials. Policy functions for investment and portfolio share are found by
 11 grid search with successive refinements.

12 The dynamic path of the GJ simulation depends on the realization of aggregate shocks.
 13 Thus we need to choose a specific path of realized outcomes of aggregate shocks to
 14 determine which GJ simulation is to be compared with the data. Here we pick the path that
 15 is closest, out of 500 Monte Carlo simulated paths at the chosen parameter values, to the
 16 Thai aggregate dynamics according to a root-mean-squared-error (RMSE) metric, defined
 17 over the aggregate paths of income growth rate, income inequality level, and fraction of
 18 participants, equally weighted.

20 A.5. PROFILES OF WEALTH AND AGGREGATE DYNAMICS



21 **FIGURE A.1.** Thai age profile of wealth by cohort: age < 30.

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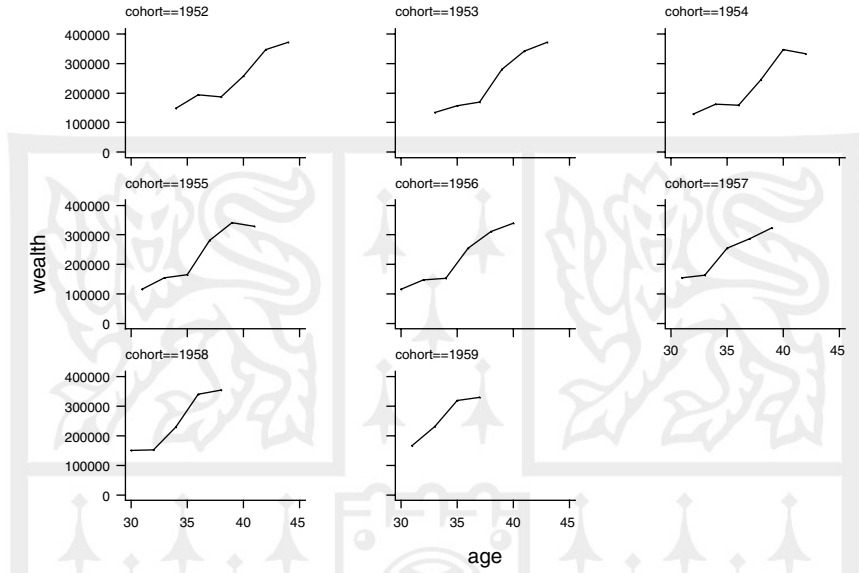


FIGURE A.2. Thai age profile of wealth by cohort: age ≥ 30 .

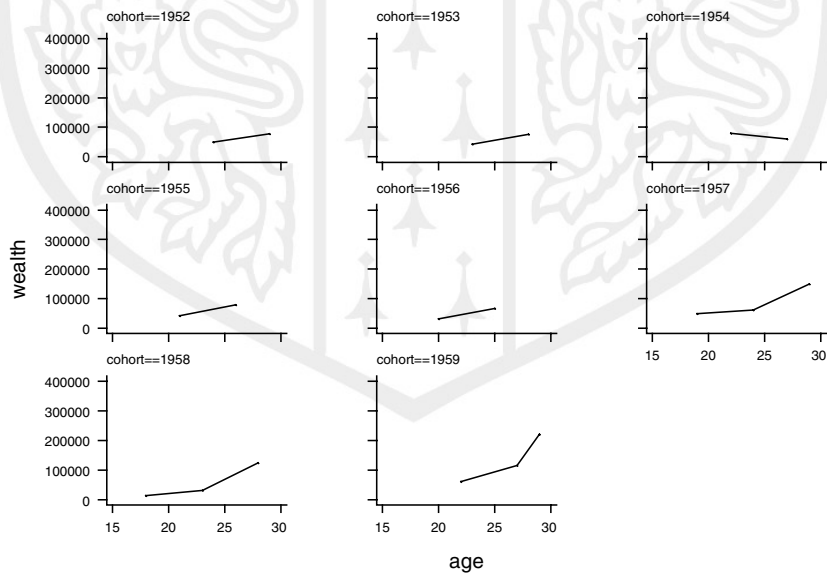


FIGURE A.3. Thai age profile of wealth of entrepreneurs by cohort: age < 30 .

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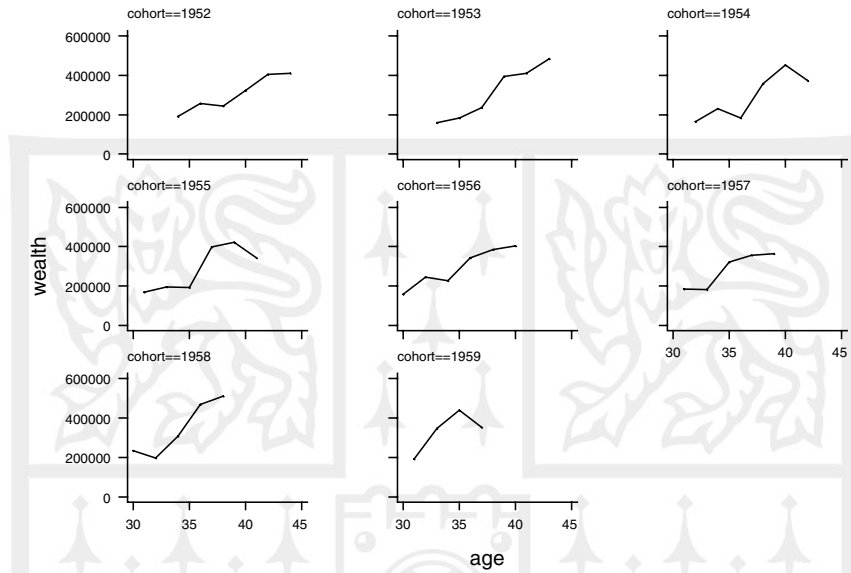


FIGURE A.4. Thai age profile of wealth of entrepreneurs by cohort: age \geq 30.

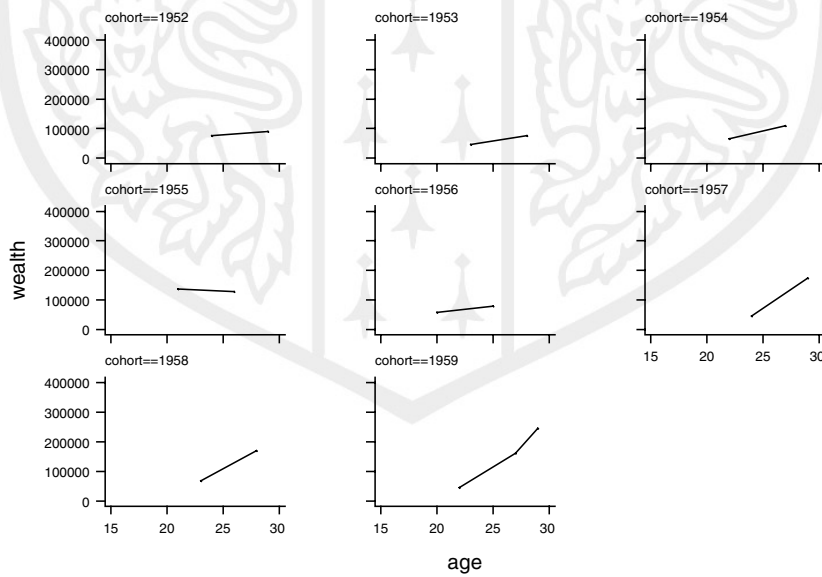


FIGURE A.5. Thai age profile of wealth of participants by cohort: age $<$ 30.

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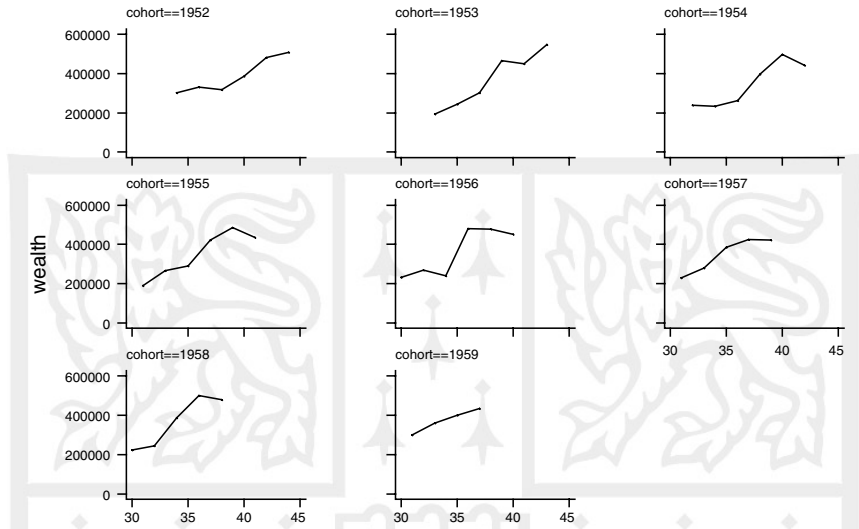


FIGURE A.6. Thai age profile of wealth of participants by cohort: age ≥ 30 .

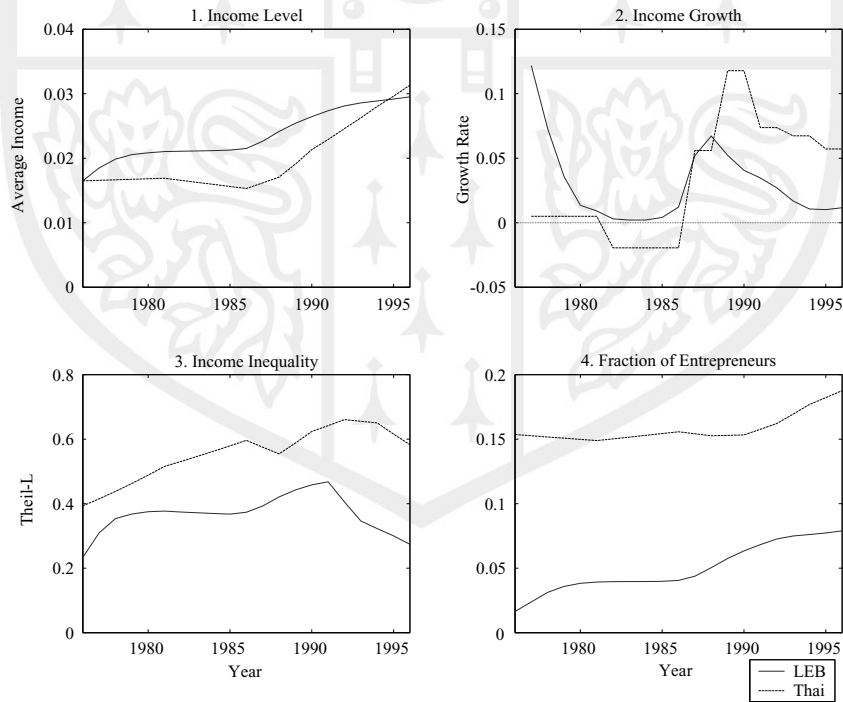


FIGURE A.7. LEB aggregate dynamics at $\alpha = 1.3$.

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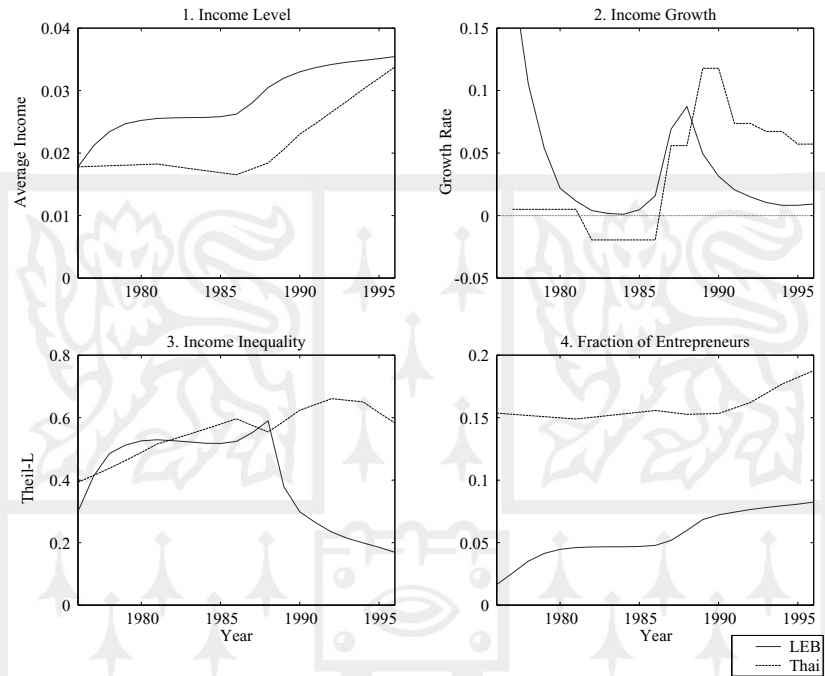


FIGURE A.8. LEB aggregate dynamics at $\xi = 0.0623$.

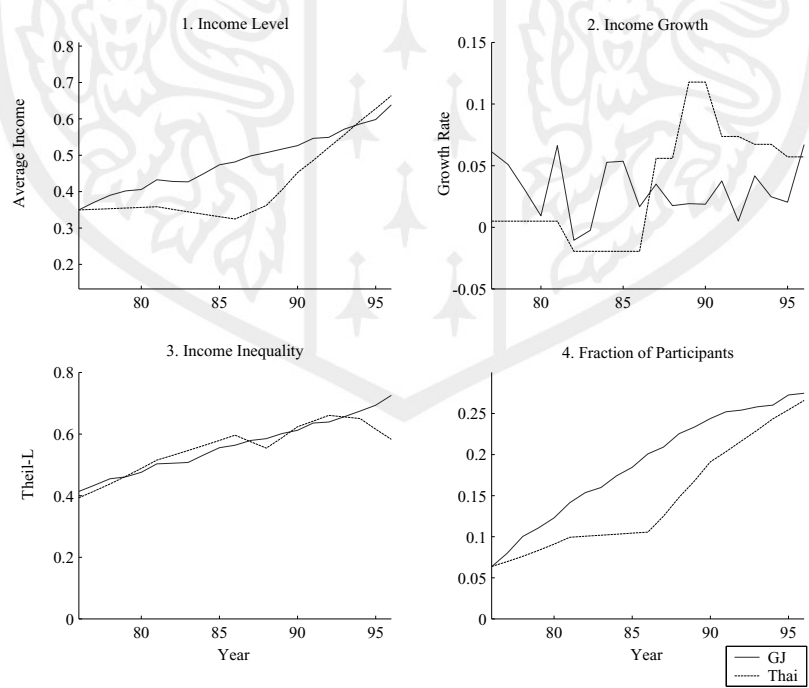


FIGURE A.9. GJ aggregate dynamics at idiosyncratic shock upper bound = 1.0309.

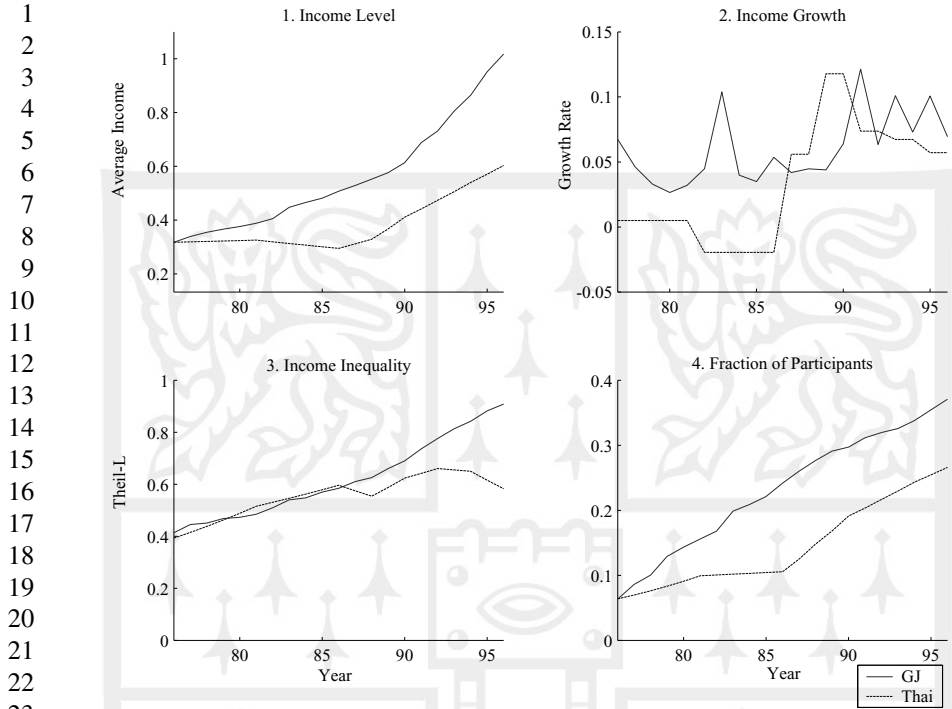


FIGURE A.10. GJ aggregate dynamics at aggregate shock lower bound = 1.0921.